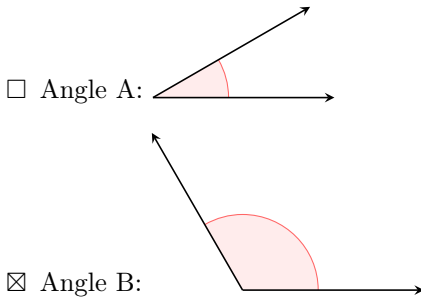


# ANGLES

## A DEFINITIONS

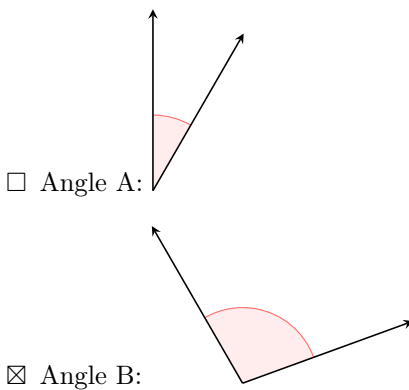
### A.1 COMPARING ANGLES

**MCQ 1:** Which angle has the greater measure?



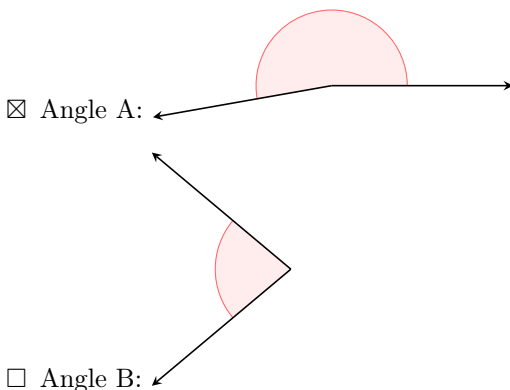
*Answer:* The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle B has a wider opening ( $120^\circ$ ) compared to Angle A ( $30^\circ$ ). Therefore, Angle B is greater.

**MCQ 2:** Which angle has the greater measure?



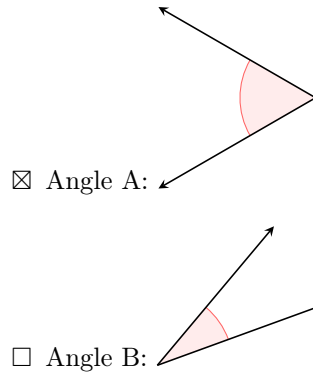
*Answer:* The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle B has a wider opening ( $100^\circ$ ) compared to Angle A ( $30^\circ$ ). Therefore, Angle B is greater.

**MCQ 3:** Which angle has the greater measure?



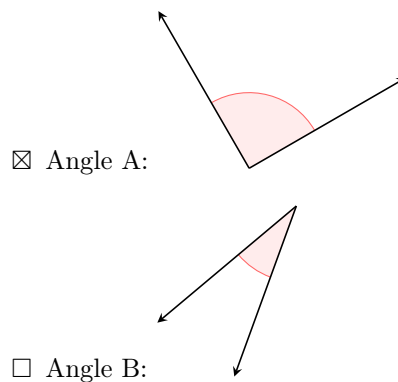
*Answer:* The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle A has a wider opening ( $170^\circ$ ) compared to Angle B ( $80^\circ$ ). Therefore, Angle A is greater.

**MCQ 4:** Which angle has the greater measure?



*Answer:* The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle A has a wider opening ( $60^\circ$ ) compared to Angle B ( $30^\circ$ ). Therefore, Angle A is greater.

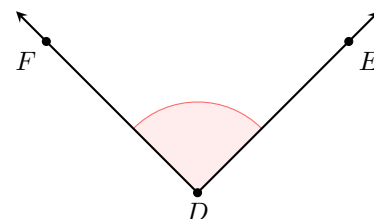
**MCQ 5:** Which angle has the greater measure?



*Answer:* The measure of an angle depends on the opening between its rays. A wider opening means a greater angle measure. Angle A has a wider opening ( $90^\circ$ ) compared to Angle B ( $30^\circ$ ). Therefore, Angle A is greater.

### A.2 NAMING ANGLES WITH THREE POINTS

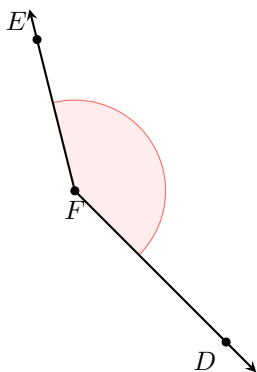
**MCQ 6:** Which option correctly names the marked angle using three-point notation?



- ☐  $\angle DEF$
- ☒  $\angle FDE$
- ☐  $\angle DFE$

*Answer:* The marked angle has vertex  $D$ , with points  $E$  and  $F$  on its sides. In three-point notation, the vertex is in the middle, so the correct name is  $\angle FDE$ .

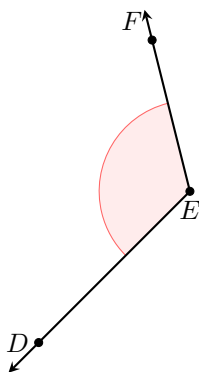
**MCQ 7:** Which option correctly names the marked angle using three-point notation?



- ☐  $\angle DEF$   
☐  $\angle FDE$   
☒  $\angle DFE$

*Answer:* The marked angle has vertex  $F$ , with points  $D$  and  $E$  on its sides. In three-point notation, the vertex is in the middle, so the correct name is  $\angle DFE$ .

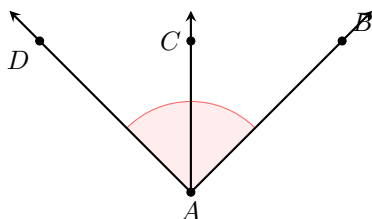
**MCQ 8:** Which option correctly names the marked angle using three-point notation?



- ☒  $\angle DEF$   
☐  $\angle FDE$   
☐  $\angle DFE$

*Answer:* The marked angle has vertex  $E$ , with points  $D$  and  $F$  on its sides. In three-point notation, the vertex is in the middle, so the correct name is  $\angle DEF$ .

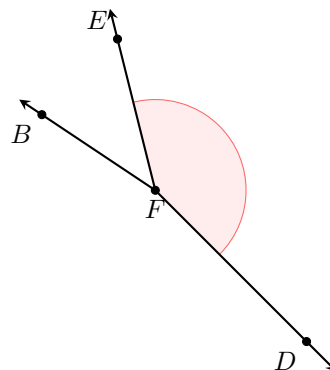
**MCQ 9:** Which option correctly names the marked angle using three-point notation?



- ☐  $\angle ADC$   
☐  $\angle CAB$   
☒  $\angle DAB$   
☐  $\angle DAC$

*Answer:* The marked angle has vertex  $A$ , with points  $D$  and  $B$  on its sides. In three-point notation, the vertex is in the middle, so the correct name is  $\angle DAB$ .

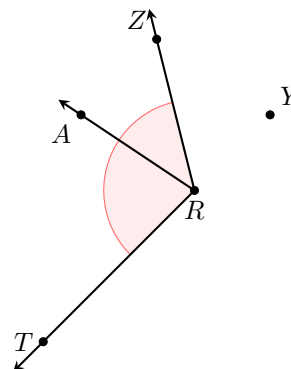
**MCQ 10:** Which option correctly names the marked angle using three-point notation?



- ☐  $\angle BFD$   
☐  $\angle FDE$   
☒  $\angle DFE$   
☐  $\angle BFE$

*Answer:* The marked angle has vertex  $F$ , with points  $D$  and  $E$  on its sides. In three-point notation, the vertex is in the middle, so the correct name is  $\angle DFE$ .

**MCQ 11:** Which option correctly names the marked angle using three-point notation?




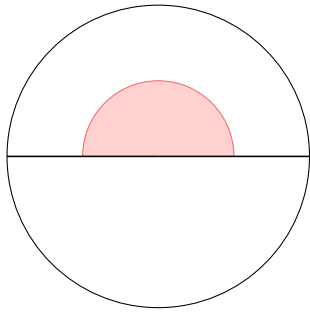
- ☐  $\angle TRY$   
☒  $\angle ZRT$   
☐  $\angle ZRA$   
☐  $\angle RZT$

*Answer:* The marked angle has vertex  $R$ , with points  $T$  and  $Z$  on its sides. In three-point notation, the vertex is in the middle, so the correct name is  $\angle ZRT$ .

## B DEGREES

### B.1 DIVIDING THE FULL TURN

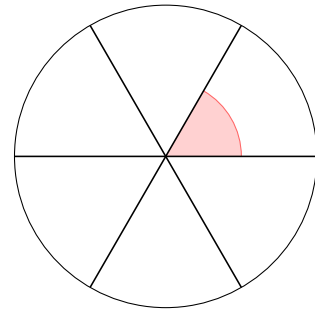
**Ex 12:** 



One-half of a full turn measures  $\boxed{180}^\circ$ .

Answer:

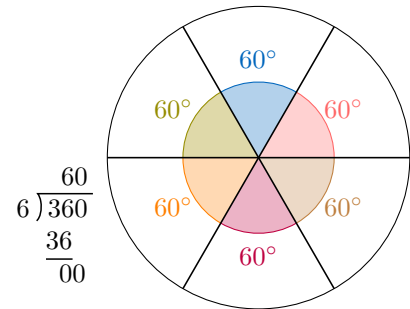
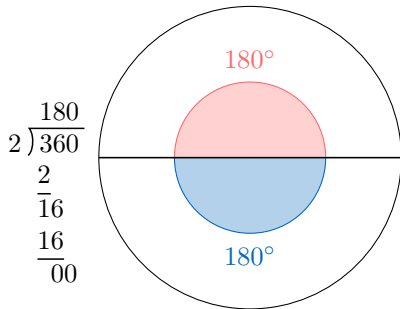
$$\begin{aligned}\text{One-half of a full turn} &= \frac{1}{2} \times 360^\circ \\ &= 360^\circ \div 2 \\ &= 180^\circ\end{aligned}$$




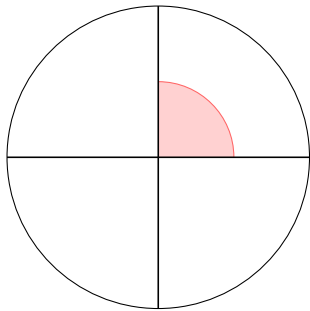
One-sixth of a full turn measures  $\boxed{60}^\circ$ .

Answer:

$$\begin{aligned}\text{One-sixth of a full turn} &= \frac{1}{6} \times 360^\circ \\ &= 360^\circ \div 6 \\ &= 60^\circ\end{aligned}$$




Ex 13: 

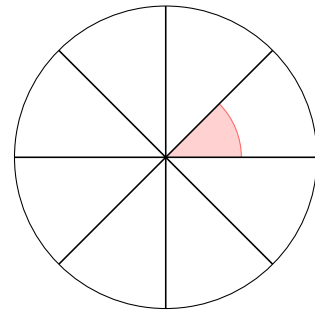


One-quarter of a full turn measures  $\boxed{90}^\circ$ .

Answer:

$$\begin{aligned}\text{One-quarter of a full turn} &= \frac{1}{4} \times 360^\circ \\ &= 360^\circ \div 4 \\ &= 90^\circ\end{aligned}$$

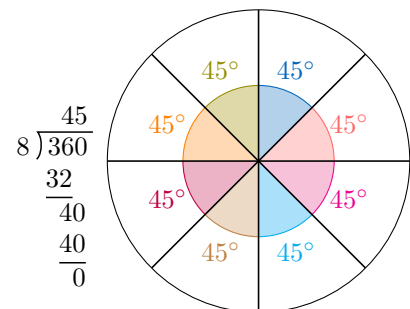
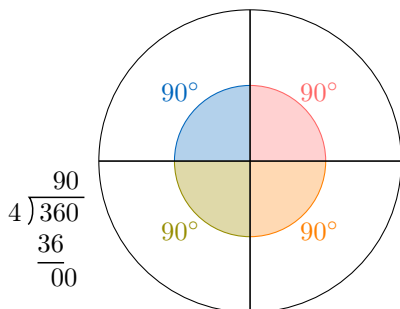
Ex 15: 





One-eighth of a full turn measures  $\boxed{45}^\circ$ .

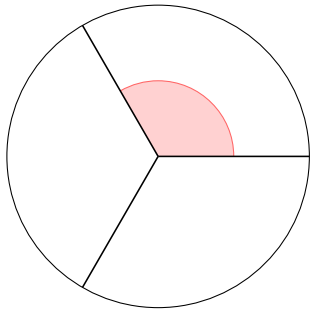
Answer:

$$\begin{aligned}\text{One-eighth of a full turn} &= \frac{1}{8} \times 360^\circ \\ &= 360^\circ \div 8 \\ &= 45^\circ\end{aligned}$$



Ex 14: 

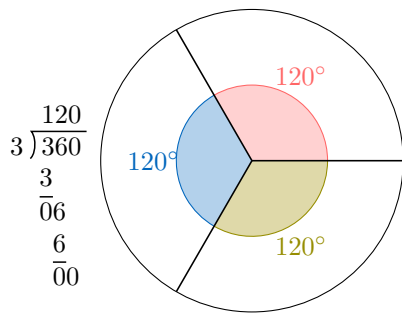
Ex 16: 



One-third of a full turn measures  $\boxed{120}^\circ$ .

*Answer:*

$$\begin{aligned}\text{One-third of a full turn} &= \frac{1}{3} \times 360^\circ \\ &= 360^\circ \div 3 \\ &= 120^\circ\end{aligned}$$

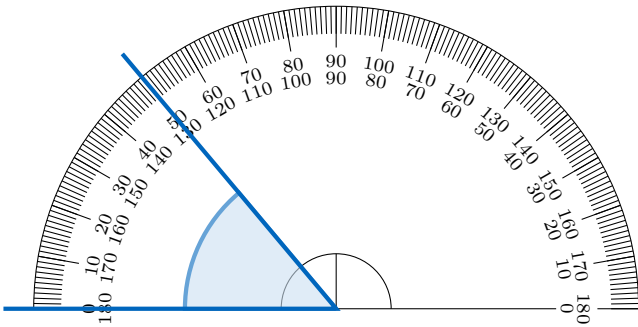


$$\begin{array}{r} 120 \\ 3 \overline{)360} \\ \underline{3} \phantom{00} \\ 06 \phantom{0} \\ \underline{6} \phantom{00} \\ 00 \end{array}$$

## C MEASURING AND DRAWING ANGLES WITH A PROTRACTOR

### C.1 MEASURING ANGLES

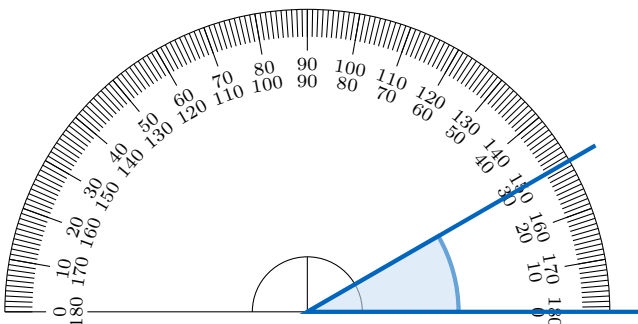
**Ex 17:**



The angle shown measures  $\boxed{50}^\circ$ .

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with  $0^\circ$ , and the other points to  $50^\circ$ , so the angle measures  $50^\circ$ .

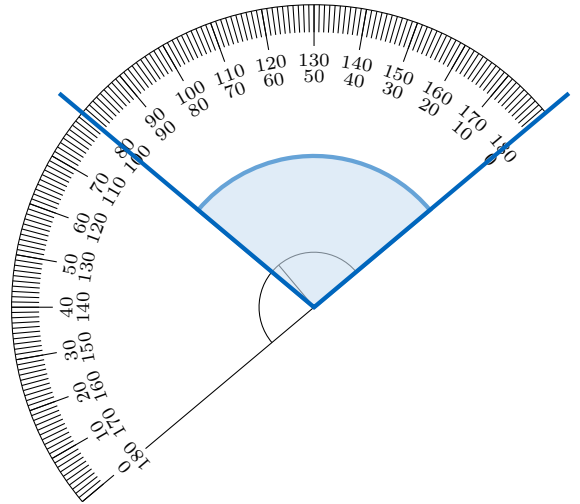
**Ex 18:**



The angle shown measures  $\boxed{30}^\circ$ .

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with  $0^\circ$ , and the other points to  $30^\circ$ , so the angle measures  $30^\circ$ .

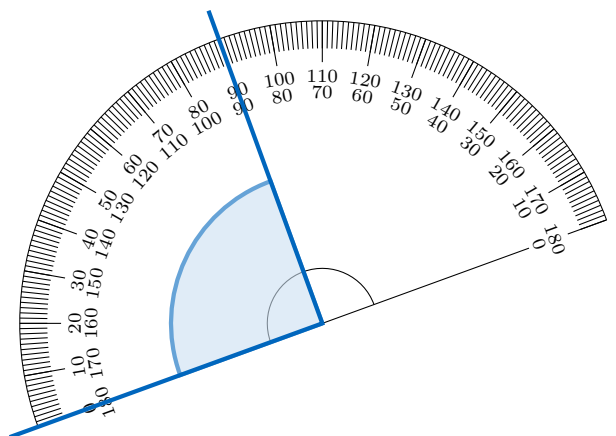
**Ex 19:**



The angle shown measures  $\boxed{100}^\circ$ .

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with  $0^\circ$ , and the other points to  $100^\circ$ , so the angle measures  $100^\circ$ .

**Ex 20:**



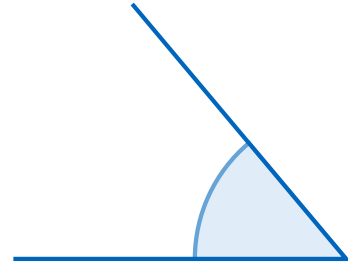
The angle shown measures  $\boxed{90}^\circ$ .

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with  $0^\circ$ , and the other points to  $90^\circ$ , so the angle measures  $90^\circ$ .

**Ex 21:**

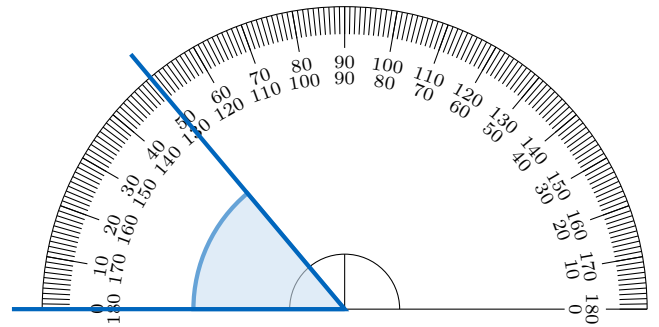
## C.2 MEASURING ANGLES

**MCQ 24:** Using a protractor, find the measure of the angle shown.



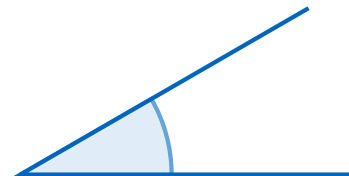
- ☐ 30°  
☒ 50°  
☐ 90°  
☐ 130°

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



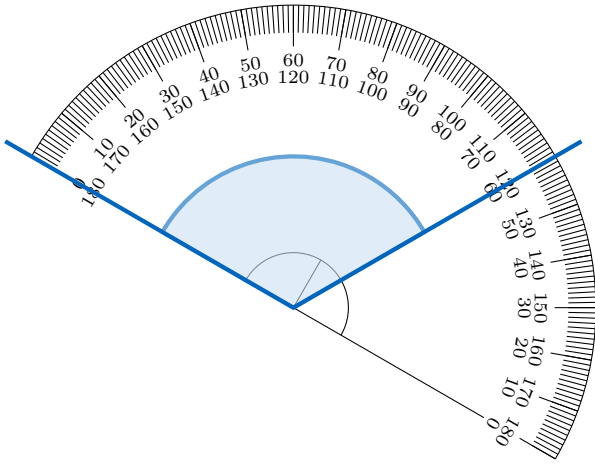
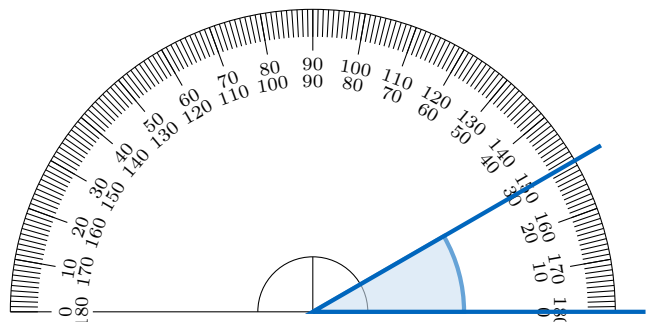
Here, one ray aligns with 0°, and the other points to 50°, so the angle measures 50°.

**MCQ 25:** Using a protractor, find the measure of the angle shown.



- ☒ 30°  
☐ 50°  
☐ 90°  
☐ 130°

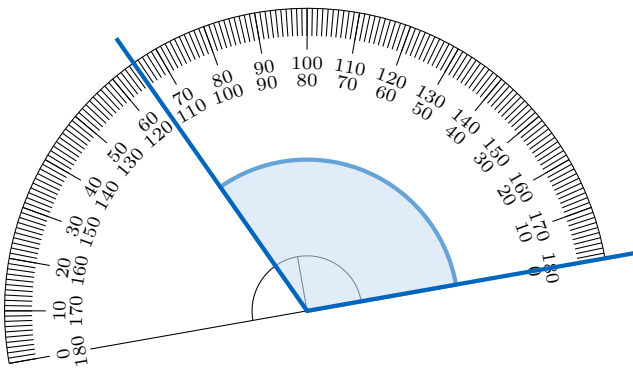
*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale.



The angle shown measures 120°.

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0°, and the other points to 120°, so the angle measures 120°.

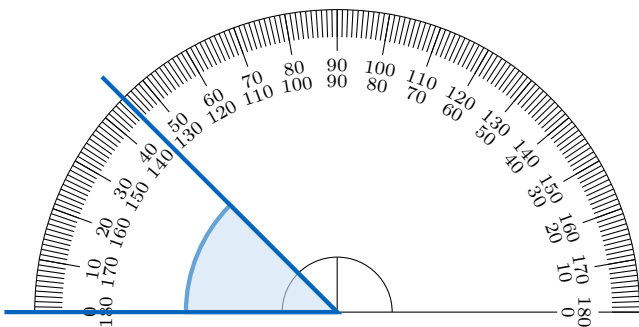
**Ex 22:**



The angle shown measures 115°.

*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0°, and the other points to 115°, so the angle measures 115°.

**Ex 23:**



The angle shown measures 45°.

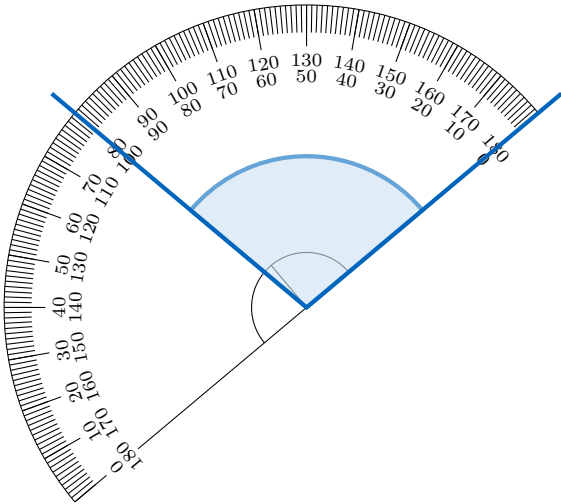
*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the 0° mark. The other ray points to the angle's measure on the protractor's scale. Here, one ray aligns with 0°, and the other points to 45°, so the angle measures 45°.

Here, one ray aligns with  $0^\circ$ , and the other points to  $30^\circ$ , so the angle measures  $30^\circ$ .

**MCQ 26:** Using a protractor, find the measure of the angle shown.

- ☐  $30^\circ$
- ☐  $50^\circ$
- ☒  $100^\circ$
- ☐  $130^\circ$

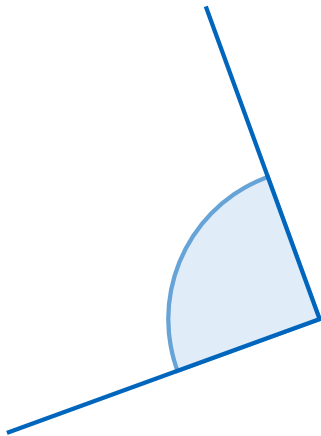
*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale.



Here, one ray aligns with  $0^\circ$ , and the other points to  $100^\circ$ , so the angle measures  $100^\circ$ .

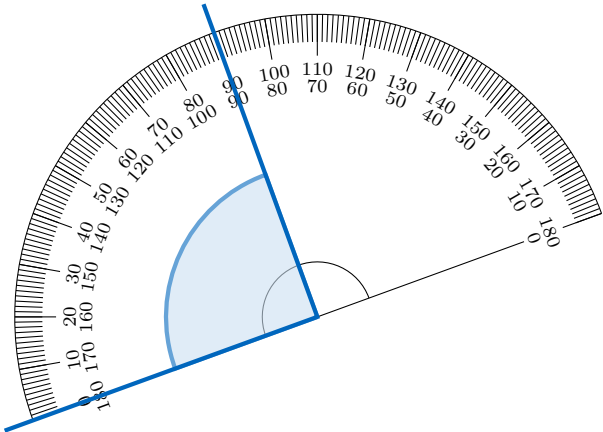
**MCQ 27:** Using a protractor, find the measure of the angle shown.

- ☐  $30^\circ$
- ☐  $50^\circ$
- ☒  $90^\circ$



☐  $130^\circ$

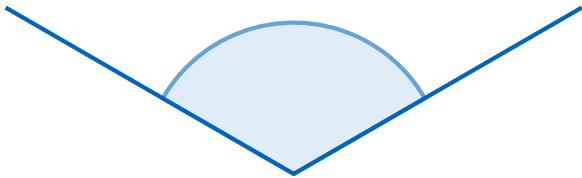
*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale.



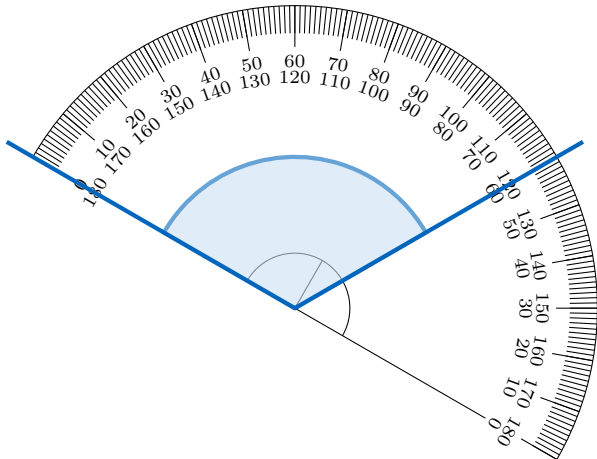
Here, one ray aligns with  $0^\circ$ , and the other points to  $90^\circ$ , so the angle measures  $90^\circ$ .

**MCQ 28:** Using a protractor, find the measure of the angle shown.

- ☐  $30^\circ$
- ☐  $50^\circ$
- ☐  $90^\circ$
- ☒  $120^\circ$



*Answer:* To measure an angle with a protractor, place its center on the vertex and align one ray with the  $0^\circ$  mark. The other ray points to the angle's measure on the protractor's scale.



Here, one ray aligns with  $0^\circ$ , and the other points to  $120^\circ$ , so the angle measures  $120^\circ$ .



### C.3 CONSTRUCTING ANGLES

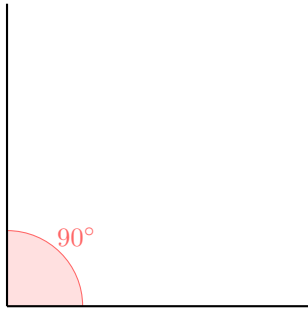
**Ex 29:** Using a pencil, a ruler, and a protractor, draw an angle that measures  $90^\circ$ .

Students should draw two rays forming an angle that measures  $90^\circ$ .

*Answer:* To draw a  $90^\circ$  angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .
3. Mark a point at  $90^\circ$  on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle measures  $90^\circ$ , as shown below.



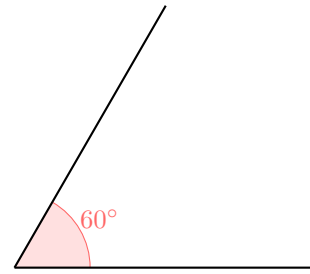
**Ex 30:** Using a pencil, a ruler, and a protractor, draw an angle that measures  $60^\circ$ .

Students should draw two rays forming an angle that measures  $60^\circ$ .

*Answer:* To draw a  $60^\circ$  angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .
3. Mark a point at  $60^\circ$  on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle measures  $60^\circ$ , as shown below.



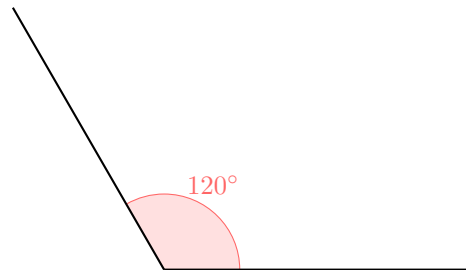
**Ex 31:** Using a pencil, a ruler, and a protractor, draw an angle that measures  $120^\circ$ .

Students should draw two rays forming an angle that measures  $120^\circ$ .

*Answer:* To draw a  $120^\circ$  angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .
3. Mark a point at  $120^\circ$  on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle measures  $120^\circ$ , as shown below.



**Ex 32:** Using a pencil, a ruler, and a protractor, draw an angle that measures  $45^\circ$ .

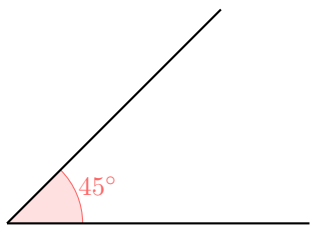
Students should draw two rays forming an angle that measures  $45^\circ$ .

*Answer:* To draw a  $45^\circ$  angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .

3. Mark a point at  $45^\circ$  on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

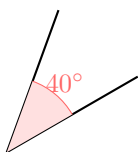
The resulting angle measures  $45^\circ$ , as shown below.



## D CLASSIFICATION OF ANGLES

### D.1 IDENTIFYING ANGLE TYPES BY MEASURE

**MCQ 33:** What is the nature of the marked angle?



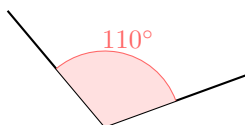
Choose one answer:

- ☒ Acute angle
- ☐ Right angle
- ☐ Obtuse angle
- ☐ Straight angle

Answer:

- An acute angle measures less than 90 degrees.
- The marked angle, measuring  $40^\circ$ , is acute because it is less than  $90^\circ$ .

**MCQ 34:** What is the nature of the marked angle?



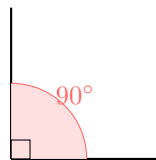
Choose one answer:

- ☐ Acute angle
- ☐ Right angle
- ☒ Obtuse angle
- ☐ Straight angle

Answer:

- An obtuse angle measures more than 90 degrees but less than 180 degrees.
- The marked angle, measuring  $110^\circ$ , is obtuse because it is between  $90^\circ$  and  $180^\circ$ .

**MCQ 35:** What is the nature of the marked angle?



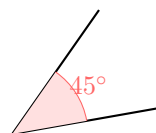
Choose one answer:

- ☐ Acute angle
- ☒ Right angle
- ☐ Obtuse angle
- ☐ Straight angle

Answer:

- A right angle measures exactly 90 degrees.
- The marked angle, measuring  $90^\circ$ , is a right angle.

**MCQ 36:** What is the nature of the marked angle?



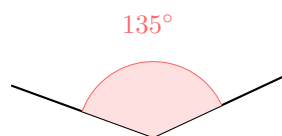
Choose one answer:

- ☒ Acute angle
- ☐ Right angle
- ☐ Obtuse angle
- ☐ Straight angle

Answer:

- An acute angle measures less than 90 degrees.
- The marked angle, measuring  $45^\circ$ , is acute because it is less than  $90^\circ$ .

**MCQ 37:** What is the nature of the marked angle?



Choose one answer:

- ☐ Acute angle
- ☐ Right angle
- ☒ Obtuse angle
- ☐ Straight angle

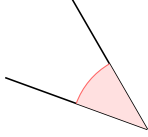
Answer:

- An obtuse angle measures more than 90 degrees but less than 180 degrees.
- The marked angle, measuring  $135^\circ$ , is obtuse because it is between  $90^\circ$  and  $180^\circ$ .



## D.2 IDENTIFYING ANGLE TYPES

**MCQ 38:** Identify the type of the highlighted angle.

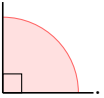


Choose one answer:

- ☒ acute angle
- ☐ right angle
- ☐ obtuse angle
- ☐ straight angle

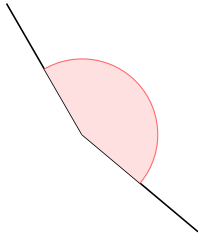
Answer:

- An acute angle measures less than  $90^\circ$ .
- The highlighted angle ( $\approx 40^\circ$ ) is less open than a right angle



- Hence it is **acute**.

**MCQ 39:** Identify the type of the highlighted angle.

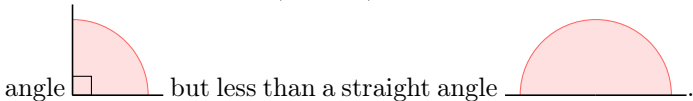


Choose one answer:

- ☐ acute angle
- ☐ right angle
- ☒ obtuse angle
- ☐ straight angle

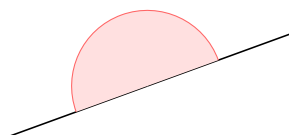
Answer:

- An obtuse angle measures between  $90^\circ$  and  $180^\circ$ .
- The highlighted angle ( $\approx 160^\circ$ ) is more open than a right angle



- Therefore it is **obtuse**.

**MCQ 40:** Identify the type of the highlighted angle.



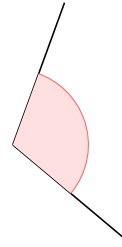
Choose one answer:

- ☐ acute angle
- ☐ right angle
- ☐ obtuse angle
- ☒ straight angle

Answer:

- A straight angle measures exactly  $180^\circ$ .
- The highlighted angle forms a line.
- It is therefore **straight**.

**MCQ 41:** Identify the type of the highlighted angle.

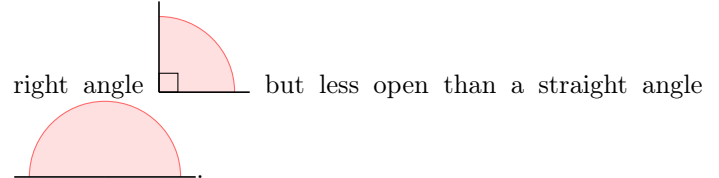


Choose one answer:

- ☐ acute angle
- ☐ right angle
- ☒ obtuse angle
- ☐ straight angle

Answer:

- An obtuse angle measures between  $90^\circ$  and  $180^\circ$ .
- The highlighted angle ( $\approx 110^\circ$ ) is more open than a



- Therefore it is **obtuse**.

## D.3 CONSTRUCTING ANGLE TYPES

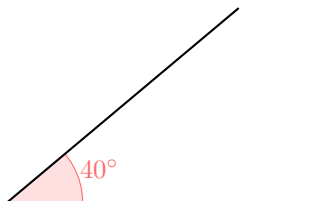
**Ex 42:** Using a pencil, a ruler, and a protractor, draw an acute angle.

Students should draw two rays forming an angle that measures less than  $90^\circ$ .

Answer: To draw an acute angle, such as a  $40^\circ$  angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .
3. Mark a point at  $40^\circ$  on the protractor's scale (any angle less than  $90^\circ$  is acceptable).
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle is acute, measuring less than  $90^\circ$ , as shown below.



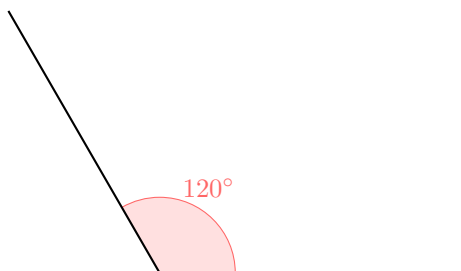
**Ex 43:** Using a pencil, a ruler, and a protractor, draw an obtuse angle.

Students should draw two rays forming an angle that measures greater than  $90^\circ$  but less than  $180^\circ$ .

*Answer:* To draw an obtuse angle, such as a  $120^\circ$  angle:

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .
3. Mark a point at  $120^\circ$  on the protractor's scale (any angle greater than  $90^\circ$  but less than  $180^\circ$  is acceptable).
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

The resulting angle is obtuse, measuring greater than  $90^\circ$  but less than  $180^\circ$ , as shown below.



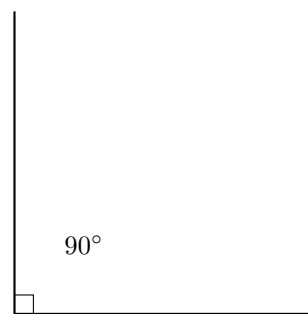
**Ex 44:** Using a pencil, a ruler, and a protractor, draw a right angle.

Students should draw two rays forming an angle that measures exactly  $90^\circ$ .

*Answer:* To draw a right angle, which measures  $90^\circ$ :

1. Draw a ray using a ruler to create the first side of the angle.
2. Place the protractor's center on the endpoint of the ray (the vertex) and align the baseline with the ray at  $0^\circ$ .
3. Mark a point at  $90^\circ$  on the protractor's scale.
4. Remove the protractor and use the ruler to draw a second ray from the vertex through the marked point.

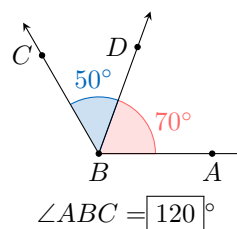
The resulting angle is a right angle, measuring exactly  $90^\circ$ , as shown below.



## E ANGLE ADDITION

### E.1 ADDING ANGLES

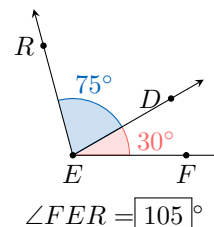
**Ex 45:** Calculate the measure of  $\angle ABC$ .



*Answer:* Using the angle addition postulate,  $\angle ABC$  is the sum of the smaller angles  $\angle ABD$  and  $\angle DBC$ :

$$\begin{aligned}\angle ABC &= \angle ABD + \angle DBC \\ &= 70^\circ + 50^\circ \\ &= 120^\circ\end{aligned}$$

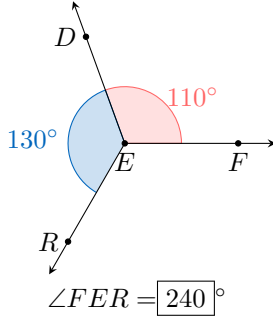
**Ex 46:** Calculate the measure of  $\angle FER$ .



*Answer:* Using the angle addition postulate,  $\angle FER$  is the sum of the smaller angles  $\angle FED$  and  $\angle DER$ :

$$\begin{aligned}\angle FER &= \angle FED + \angle DER \\ &= 30^\circ + 75^\circ \\ &= 105^\circ\end{aligned}$$

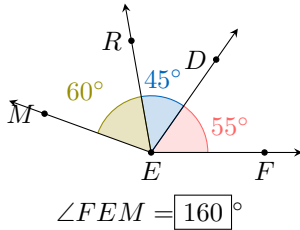
**Ex 47:** Calculate the measure of  $\angle FER$ .



*Answer:* Using the angle addition postulate,  $\angle FER$  is the sum of the smaller angles  $\angle FED$  and  $\angle DER$ :

$$\begin{aligned}\angle FER &= \angle FED + \angle DER \\ &= 110^\circ + 130^\circ \\ &= 240^\circ\end{aligned}$$

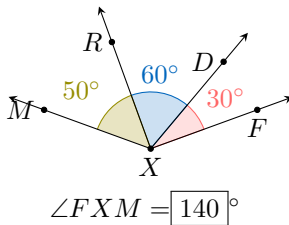
**Ex 48:** Calculate the measure of  $\angle FEM$ .



*Answer:* Using the angle addition postulate,  $\angle FEM$  is the sum of the smaller angles  $\angle FED$ ,  $\angle DER$ , and  $\angle REM$ :

$$\begin{aligned}\angle FEM &= \angle FED + \angle DER + \angle REM \\ &= 55^\circ + 45^\circ + 60^\circ \\ &= 160^\circ\end{aligned}$$

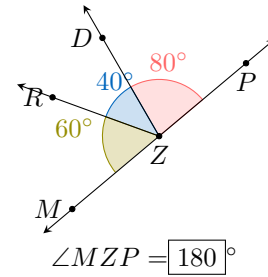
**Ex 49:** Calculate the measure of  $\angle FXM$ .



*Answer:* Using the angle addition postulate,  $\angle FXM$  is the sum of the smaller angles  $\angle FXD$ ,  $\angle DXR$ , and  $\angle RXM$ :

$$\begin{aligned}\angle FXM &= \angle FXD + \angle DXR + \angle RXM \\ &= 30^\circ + 60^\circ + 50^\circ \\ &= 140^\circ\end{aligned}$$

**Ex 50:** Calculate the measure of  $\angle MZP$ .

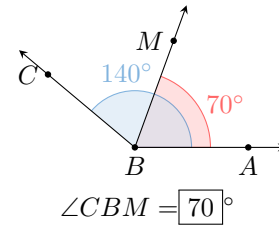


*Answer:* Using the angle addition postulate,  $\angle MZP$  is the sum of the smaller angles  $\angle MZR$ ,  $\angle RZD$ , and  $\angle DZP$ :

$$\begin{aligned}\angle MZP &= \angle MZR + \angle RZD + \angle DZP \\ &= 60^\circ + 40^\circ + 80^\circ \\ &= 180^\circ\end{aligned}$$

## E.2 SUBTRACTING ANGLE

**Ex 51:** Calculate the measure of  $\angle CBM$ .



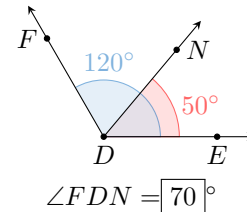
*Answer:* Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle CBM + \angle MBA = \angle CBA$$

To find  $\angle CBM$ , subtract  $\angle MBA$  from  $\angle CBA$ :

$$\begin{aligned}\angle CBM &= \angle CBA - \angle MBA \\ &= 140^\circ - 70^\circ \\ &= 70^\circ\end{aligned}$$

**Ex 52:** Calculate the measure of  $\angle FDN$ .



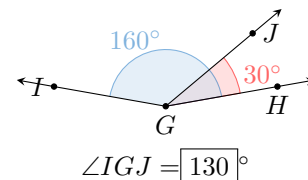
*Answer:* Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle FDN + \angle NDE = \angle FDE$$

To find  $\angle FDN$ , subtract  $\angle NDE$  from  $\angle FDE$ :

$$\begin{aligned}\angle FDN &= \angle FDE - \angle NDE \\ &= 120^\circ - 50^\circ \\ &= 70^\circ\end{aligned}$$

**Ex 53:** Calculate the measure of  $\angle IGJ$ .



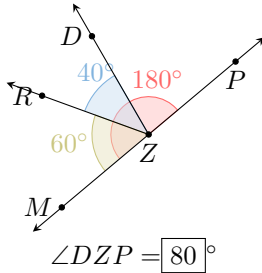
*Answer:* Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle IGJ + \angle JGH = \angle IGH$$

To find  $\angle IGJ$ , subtract  $\angle JGH$  from  $\angle IGH$ :

$$\begin{aligned}\angle IGJ &= \angle IGH - \angle JGH \\ &= 160^\circ - 30^\circ \\ &= 130^\circ\end{aligned}$$

**Ex 54:** Calculate the measure of  $\angle DZP$  by subtracting the known angles from the larger angle using the angle addition postulate.



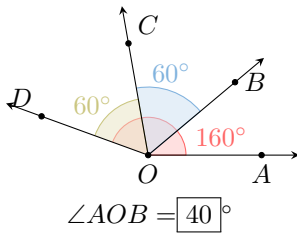
*Answer:* Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle MZR + \angle RZD + \angle DZP = \angle MZP$$

To find  $\angle DZP$ , subtract  $\angle MZR$  and  $\angle RZD$  from  $\angle MZP$ :

$$\begin{aligned}\angle DZP &= \angle MZP - \angle MZR - \angle RZD \\ &= 180^\circ - 60^\circ - 40^\circ \\ &= 80^\circ\end{aligned}$$

**Ex 55:** Calculate the measure of  $\angle AOB$  by subtracting the known angles from the larger angle using the angle addition postulate.



*Answer:* Using the angle addition postulate, the larger angle is the sum of the smaller angles:

$$\angle AOB + \angle BOC + \angle COD = \angle AOD$$

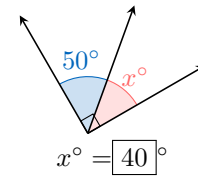
To find  $\angle AOB$ , subtract  $\angle BOC$  and  $\angle COD$  from  $\angle AOD$ :

$$\begin{aligned}\angle AOB &= \angle AOD - \angle BOC - \angle COD \\ &= 160^\circ - 60^\circ - 60^\circ \\ &= 40^\circ\end{aligned}$$

## F ANGLE PROPERTIES

### F.1 CALCULATING AN UNKNOWN ANGLE IN A RIGHT ANGLE

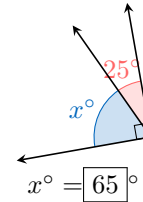
**Ex 56:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a right angle is equal to  $90^\circ$ .

$$\begin{aligned}x^\circ + 50^\circ &= 90^\circ \\ x^\circ &= 90^\circ - 50^\circ \quad (\text{subtract } 50^\circ) \\ &= 40^\circ\end{aligned}$$

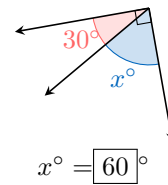
**Ex 57:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a right angle is equal to  $90^\circ$ .

$$\begin{aligned}25^\circ + x^\circ &= 90^\circ \\ x^\circ &= 90^\circ - 25^\circ \quad (\text{subtract } 25^\circ) \\ &= 65^\circ\end{aligned}$$

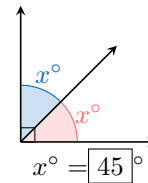
**Ex 58:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a right angle is equal to  $90^\circ$ .

$$\begin{aligned}30^\circ + x^\circ &= 90^\circ \\ x^\circ &= 90^\circ - 30^\circ \quad (\text{subtract } 30^\circ) \\ &= 60^\circ\end{aligned}$$

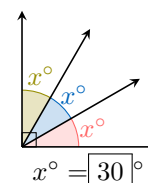
**Ex 59:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a right angle is equal to  $90^\circ$ . The two angles are equal ( $x^\circ$ ).

$$\begin{aligned}x^\circ + x^\circ &= 90^\circ \\ 2x^\circ &= 90^\circ \quad (\text{combine like terms}) \\ x^\circ &= 90^\circ \div 2 \quad (\text{divide by } 2) \\ &= 45^\circ\end{aligned}$$

**Ex 60:** Calculate the measure of the unknown angle.

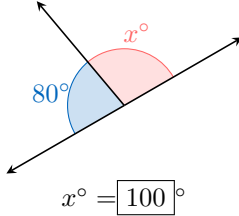


*Answer:* The sum of angles in a right angle is equal to  $90^\circ$ . The three angles are equal ( $x^\circ$ ).

$$\begin{aligned}x^\circ + x^\circ + x^\circ &= 90^\circ \\3x^\circ &= 90^\circ \quad (\text{combine like terms}) \\x^\circ &= 90^\circ \div 3 \quad (\text{divide by 3}) \\&= 30^\circ\end{aligned}$$

## F.2 CALCULATING AN UNKNOWN ANGLE IN A STRAIGHT ANGLE

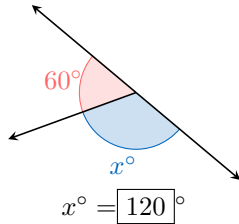
**Ex 61:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a straight line is equal to  $180^\circ$ .

$$\begin{aligned}x^\circ + 80^\circ &= 180^\circ \\x^\circ &= 180^\circ - 80^\circ \quad (\text{subtract } 80^\circ) \\&= 100^\circ\end{aligned}$$

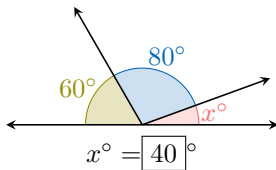
**Ex 62:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a straight line is equal to  $180^\circ$ .

$$\begin{aligned}60^\circ + x^\circ &= 180^\circ \\x^\circ &= 180^\circ - 60^\circ \quad (\text{subtract } 60^\circ) \\&= 120^\circ\end{aligned}$$

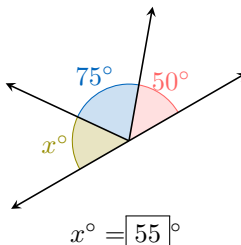
**Ex 63:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a straight line is equal to  $180^\circ$ .

$$\begin{aligned}x^\circ + 80^\circ + 60^\circ &= 180^\circ \\x^\circ &= 180^\circ - 80^\circ - 60^\circ \quad (\text{subtract } 80^\circ \text{ and } 60^\circ) \\&= 40^\circ\end{aligned}$$

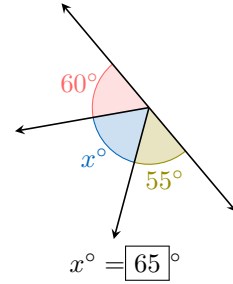
**Ex 64:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a straight line is equal to  $180^\circ$ .

$$\begin{aligned}50^\circ + 75^\circ + x^\circ &= 180^\circ \\x^\circ &= 180^\circ - 50^\circ - 75^\circ \quad (\text{subtract } 50^\circ \text{ and } 75^\circ) \\&= 55^\circ\end{aligned}$$

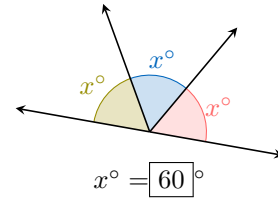
**Ex 65:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a straight line is equal to  $180^\circ$ .

$$\begin{aligned}60^\circ + x^\circ + 55^\circ &= 180^\circ \\x^\circ &= 180^\circ - 60^\circ - 55^\circ \quad (\text{subtract } 60^\circ \text{ and } 55^\circ) \\&= 65^\circ\end{aligned}$$

**Ex 66:** Calculate the measure of the unknown angle.

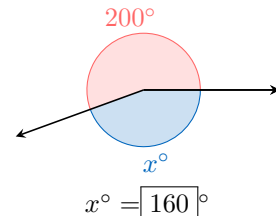


*Answer:* The sum of angles in a straight line is equal to  $180^\circ$ . The three angles are equal ( $x^\circ$ ).

$$\begin{aligned}x^\circ + x^\circ + x^\circ &= 180^\circ \\3x^\circ &= 180^\circ \quad (\text{combine like terms}) \\x^\circ &= 180^\circ \div 3 \quad (\text{divide by 3}) \\&= 60^\circ\end{aligned}$$

## F.3 CALCULATING AN UNKNOWN ANGLE IN A FULL ANGLE

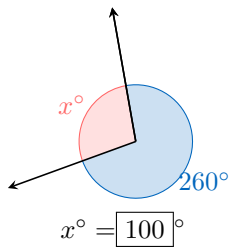
**Ex 67:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a point is equal to  $360^\circ$ .

$$\begin{aligned}200^\circ + x^\circ &= 360^\circ \\x^\circ &= 360^\circ - 200^\circ \quad (\text{subtract } 200^\circ) \\&= 160^\circ\end{aligned}$$

**Ex 68:** Calculate the measure of the unknown angle.

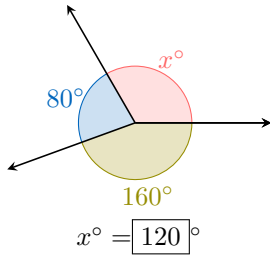


*Answer:* The sum of angles in a point is equal to  $360^\circ$ .

$$x^\circ + 260^\circ = 360^\circ$$

$$\begin{aligned} x^\circ &= 360^\circ - 260^\circ \quad (\text{subtract } 260^\circ) \\ &= 100^\circ \end{aligned}$$

**Ex 69:** Calculate the measure of the unknown angle.

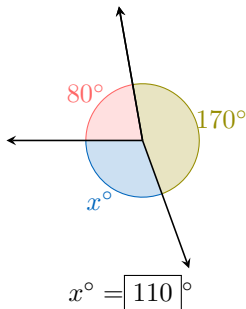


*Answer:* The sum of angles in a point is equal to  $360^\circ$ .

$$x^\circ + 80^\circ + 160^\circ = 360^\circ$$

$$\begin{aligned} x^\circ &= 360^\circ - 80^\circ - 160^\circ \quad (\text{subtract } 80^\circ \text{ and } 160^\circ) \\ &= 120^\circ \end{aligned}$$

**Ex 70:** Calculate the measure of the unknown angle.

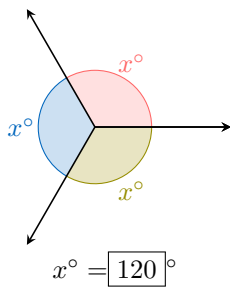


*Answer:* The sum of angles in a point is equal to  $360^\circ$ .

$$80^\circ + x^\circ + 170^\circ = 360^\circ$$

$$\begin{aligned} x^\circ &= 360^\circ - 80^\circ - 170^\circ \quad (\text{subtract } 80^\circ \text{ and } 170^\circ) \\ &= 110^\circ \end{aligned}$$

**Ex 71:** Calculate the measure of the unknown angle.



*Answer:* The sum of angles in a point is equal to  $360^\circ$ . The three angles are equal ( $x^\circ$ ).

$$x^\circ + x^\circ + x^\circ = 360^\circ$$

$$3x^\circ = 360^\circ \quad (\text{combine like terms})$$

$$\begin{aligned} x^\circ &= 360^\circ \div 3 \quad (\text{divide by } 3) \\ &= 120^\circ \end{aligned}$$