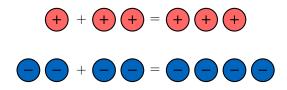
INTEGERS

A DEFINITION

Discover: On a distant planet, two tribes are at war: the **positives** and the **negatives**.

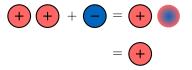
• When troops from the same tribe meet, they unite.



• When a **positive** and a **negative** meet, they cancel each other out.



• Let's see what happens if 2 positives meet 1 negative,

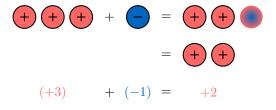


There remains 1 positive.

- To show which tribe the number belongs to, we put a sign in front of the number:
 - The + sign for the tribe of **positives**.



- The sign for the tribe of **negatives**.
 - -3 = -
- Now, let's see what happens when **3 positives** meet **1 negative**.



There remains 2 positives.

• Finally, let's see what happens when **2** positives meet **2** negatives.



There remains 0.

Definition Positive and Negative Numbers _

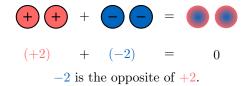
• Positive numbers are $+1, +2, \ldots$ We write them with a positive sign (+) before the number:



• Negative numbers are $-1, -2, \ldots$ We write them with a negative sign (-) before the number:



• Positive numbers are the opposite of negative numbers:



• Integer numbers are positive numbers, negative numbers, and zero :

 $\ldots, -3, -2, -1, 0, +1, +2, +3, \ldots$

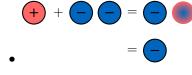
• Positive numbers can be written with or without a positive sign (+) in front of the number:



- To avoid confusion between the sign of the number and the sign of the operation, we can use parentheses. For example, +1 + -2 becomes (+1) + (-2).
- 0 is neither positive nor negative.

Ex: Calculate
$$(+1) + (-2)$$
.

Answer:



• So, (+1) + (-2) = -1.

Definition Absolute Value -

The absolute value of a number is the number without its sign.

- The absolute value of $+2 = \textcircled{\bullet} \textcircled{\bullet}$ is 2.
- The absolute value of $-3 = \bigcirc \bigcirc \bigcirc$ is 3.

B RULES OF ADDITION

Method Rules of Addition

• When you add two positive numbers, add their absolute values. The sum is also a positive number.

$$(+2) + (+7) = +9$$
 as $2 + 7 = 9$

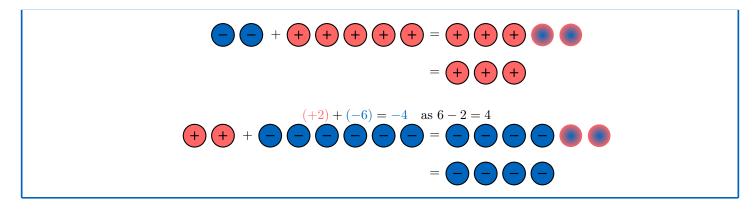
• When you add two negative numbers, add their absolute values. The sum is also a negative number.

$$(-5) + (-10) = -15$$
 as $5 + 10 = 15$

• When you add a **positive number** and a **negative number**, subtract the smaller absolute value from the larger one and use the sign of the number with the larger absolute value.

$$(-2) + (+5) = +3$$
 as $5-2=3$





Ex: Calculate (-10) + (+3)

Answer:

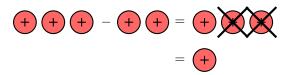
• (-10) + (+3) = -7 as 10 - 3 = 7

$\mathbf{O} = \mathbf{O} =$

C SUBTRACTION

Discover:

• - For the subtraction, (+3) - (+2):



we remove 2 positives from 3 positives, leaving us with 1 positive.

- For the addition, (+3) + (-2):



we remove again 2 positives from 3 positives.

- Therefore, these two operations are equivalent:

(+3) - (+2) = (+3) + (-2)



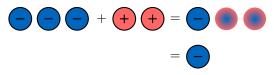
This shows that subtracting a positive number is the same as adding its opposite.

- For the subtraction, (-3) - (-2):



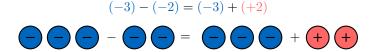
we remove 2 negatives from 3 negatives, leaving us with 1 negative.

- For the addition, (-3) + (+2):



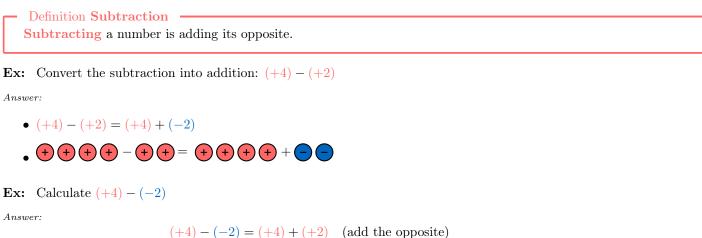
- we remove again 2 negatives from 3 negatives.
- Therefore, these two operations are equivalent:





This shows that subtracting a negative number is the same as adding its opposite.

• In conclusion, these examples show a fundamental principle of arithmetic: subtracting any number is equivalent to adding the number with its opposite sign.



(add the opposite) (same sign: add the absolute values)

D ON THE NUMBER LINE

Discover:

• To show both positive and negative numbers on a number line, we extend the number line in both directions from zero.

• For each move from left to right by 1, the number increases by 1: 0 + 1 = +1, +1 + 1 = +2, ...

$$+1$$
 $+1$ $+1$ $+1$ $+1$ $+1$ $+1$ $+1$
0 $+1$ $+2$ $+3$ $+4$ $+5$ $+6$

• For each move from right to left by 1, the number decreases by 1: 0 - 1 = -1, -1 - 1 = -2, ...

Definition Number line -

A number line is a straight line with markings at equal intervals to denote the numbers.

$$-6$$
 -5 -4 -3 -2 -1 0 $+1$ $+2$ $+3$ $+4$ $+5$ $+6$

Ex: Find the value of x.

$$\xrightarrow{x}$$

Answer:

• So, x = -2.

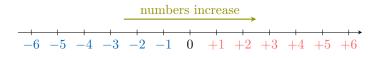


E ORDERING

Discover: In the set of numbers, the order is defined as:

 $\ldots < -3 < -2 < -1 < 0 < +1 < +2 < +3 < \ldots$

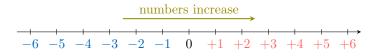
So, as you move along the number line from left to right, the numbers increase.



- As +3 is to the right of -5, -5 < +3. So, when one number is **positive** and the other is **negative**, the positive number is **greater**.
- As -2 is to the right of -4, -4 < -2. So, when both numbers are **negative**, the number closer to zero is **greater** (the number with the smaller absolute value is greater).
- As +6 is to the right of +4, +4 < +6. So, when both numbers are **positive**, the number further from zero is **greater** (the number with the greater absolute value is greater).

Method Compare two numbers _

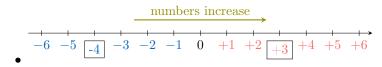
- When one number is **positive** and the other is **negative**, the positive number is **greater**.
- When both numbers are **negative**, the number closer to zero is **greater** (the number with the smaller absolute value is greater).
- When both numbers are **positive**, the number further from zero is **greater** (the number with the greater absolute value is greater).



Ex: Compare -4 and +3

Answer:

• As +3 is positive and -4 is negative, the positive number is greater than the negative number: -4 < +3



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