

# INTEGERS

## A DEFINITION

### A.1 COUNTING POSITIVE AND NEGATIVE NUMBERS

Ex 1:

$$\textcircled{+} \textcircled{+} = \boxed{\phantom{00}}$$

Ex 2:

$$\textcircled{-} \textcircled{-} \textcircled{-} = \boxed{\phantom{00}}$$

Ex 3:

$$\textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} \textcircled{-} = \boxed{\phantom{00}}$$

Ex 4:

$$\textcircled{+} \textcircled{+} \textcircled{+} = \boxed{\phantom{00}}$$

Ex 5:

$$\textcircled{-} = \boxed{\phantom{00}}$$

### A.2 WRITING INTEGERS FROM WORDS

Ex 6: Positive two is  $\boxed{\phantom{00}}$ .

Ex 7: Negative three is  $\boxed{\phantom{00}}$ .

Ex 8: Negative four is  $\boxed{\phantom{00}}$ .

Ex 9: Positive five is  $\boxed{\phantom{00}}$ .

Ex 10: Negative two is  $\boxed{\phantom{00}}$ .

### A.3 FINDING THE OPPOSITE

Ex 11: The opposite of  $-4$  is  $\boxed{\phantom{00}}$ .

Ex 12: The opposite of  $-3$  is  $\boxed{\phantom{00}}$ .

Ex 13: The opposite of  $+5$  is  $\boxed{\phantom{00}}$ .

Ex 14: The opposite of  $+1$  is  $\boxed{\phantom{00}}$ .

Ex 15: The opposite of 0 is  $\boxed{\phantom{00}}$ .

### A.4 FINDING THE OPPOSITE FOR DECIMAL NUMBERS

Ex 16: The opposite of  $-4.1$  is  $\boxed{\phantom{00}}$ .

Ex 17: The opposite of  $-0.5$  is  $\boxed{\phantom{00}}$ .

Ex 18: The opposite of  $+3.5$  is  $\boxed{\phantom{00}}$ .

Ex 19: The opposite of  $+99.5$  is  $\boxed{\phantom{00}}$ .

### A.5 ADDING SMALL INTEGERS

Ex 20:  $(+1) + (-2) = \boxed{\phantom{00}}$

Ex 21:  $(+3) + (-1) = \boxed{\phantom{00}}$

Ex 22:  $(+2) + (-3) = \boxed{\phantom{00}}$

Ex 23:  $(-2) + (-1) = \boxed{\phantom{00}}$

Ex 24:  $(-1) + (+3) = \boxed{\phantom{00}}$

Ex 25:  $(+2) + (+3) = \boxed{\phantom{00}}$

### A.6 FINDING MISSING NUMBERS IN ADDITION

Ex 26:  $(+3) + (\boxed{\phantom{00}}) = +1$

Ex 27:  $(-4) + (\boxed{\phantom{00}}) = -2$

Ex 28:  $(\boxed{\phantom{00}}) + (+2) = -1$

Ex 29:  $(-2) + (\boxed{\phantom{00}}) = -5$

Ex 30:  $(\boxed{\phantom{00}}) + (+1) = +3$

Ex 31:  $(+2) + (\boxed{\phantom{00}}) = -3$

### A.7 FINDING THE ABSOLUTE VALUE

Ex 32: The absolute value of  $+2$  is  $\boxed{\phantom{00}}$ .

Ex 33: The absolute value of  $-3$  is  $\boxed{\phantom{00}}$ .

Ex 34: The absolute value of  $+5$  is  $\boxed{\phantom{00}}$ .

Ex 35: The absolute value of  $-4$  is  $\boxed{\phantom{00}}$ .

Ex 36: The absolute value of  $-9$  is  $\boxed{\phantom{00}}$ .

### A.8 FINDING THE ABSOLUTE VALUE FOR DECIMAL NUMBERS

Ex 37: The absolute value of  $-2.1$  is  $\boxed{\phantom{00}}$ .

Ex 38: The absolute value of  $-5.4$  is  $\boxed{\phantom{00}}$ .

Ex 39: The absolute value of  $3.7$  is  $\boxed{\phantom{00}}$ .

Ex 40: The absolute value of 0 is  $\boxed{\phantom{00}}$ .

## B RULES OF ADDITION

### B.1 ADDING INTEGERS

Ex 41:  $(+6) + (-4) = \boxed{\phantom{00}}$

Ex 42:  $(+4) + (+7) = \boxed{\phantom{00}}$

Ex 43:  $(-5) + (+8) = \boxed{\phantom{00}}$

Ex 44:  $(+6) + (-4) = \boxed{\phantom{00}}$

Ex 45:  $(-5) + (-4) = \boxed{\phantom{00}}$

## B.2 ADDING INTEGERS WITHOUT EXPLICIT SIGNS

Ex 46:  $6 + (-4) = \boxed{\phantom{00}}$

Ex 47:  $-5 + 8 = \boxed{\phantom{00}}$

Ex 48:  $-2 + (-3) = \boxed{\phantom{00}}$

Ex 49:  $-6 + 0 = \boxed{\phantom{00}}$

## B.3 ADDING SIGNED DECIMAL NUMBERS

Ex 50:  $-5 + 8.1 = \boxed{\phantom{00}}$

Ex 51:  $-3 + (-2.5) = \boxed{\phantom{00}}$

Ex 52:  $-1.6 + (+2.6) = \boxed{\phantom{00}}$

Ex 53:  $-3.5 + (+1.5) = \boxed{\phantom{00}}$

## B.4 ADDING MULTIPLE INTEGERS

Ex 54: Calculate:

$$(+3) + (-7) + (-5) = \boxed{\phantom{00}}$$

Ex 55: Calculate:

$$(-2) + (-4) + (+7) = \boxed{\phantom{00}}$$

Ex 56: Calculate:

$$(-2) + (+4) + (-2) = \boxed{\phantom{00}}$$

Ex 57: Calculate:

$$(-10) + (+3) + (-7) = \boxed{\phantom{00}}$$

## B.5 ADDING INTEGERS IN REAL-WORLD PROBLEMS

Ex 58: During a hike, the hiker experiences altitude changes as follows. Positive numbers indicate climbing (gaining altitude), while negative numbers indicate descending (losing altitude):

- The hiker starts at an altitude of +300 meters.
- They climb +150 meters in the morning.
- In the afternoon, they descend by -200 meters.

What is the hiker's final altitude at the end of the day?

$\boxed{\phantom{00}}$  meters

Ex 59: A person keeps track of their bank account balance as follows. Positive numbers indicate deposits (money added), while negative numbers indicate withdrawals (money taken out):

- The person starts with +50 dollars in their account.
- They deposit +30 dollars.
- Later, they withdraw -40 dollars.

What is the person's final balance?

$\boxed{\phantom{00}}$  dollars

Ex 60: In a round of golf, each hole has a "par" score, and a player's score is based on how many strokes they take compared to par. A score of 0 means the player made par, a positive number means they took extra strokes (over par), and a negative number means they made fewer strokes (under par).

- Hole 1: Par 3, player scored -1 (under par)
- Hole 2: Par 4, player scored +2 (over par)
- Hole 3: Par 5, player scored 0 (made par)
- Hole 4: Par 3, player scored +1 (over par)
- Hole 5: Par 4, player scored -2 (under par)

What is the player's total score?

$\boxed{\phantom{00}}$

Ex 61: Throughout the day, the temperature in a city changes as follows. Positive numbers indicate a rise in temperature, while negative numbers indicate a drop in temperature:

- In the morning, the temperature started at +5°C and dropped by -3°C.
- In the afternoon, the temperature rose by +4°C.
- In the evening, the temperature dropped again by -6°C.
- At night, it dropped further by -1°C.

What is the temperature at the end of the day?

$\boxed{\phantom{00}}^{\circ}\text{C}$

## C SUBTRACTION

### C.1 CONVERTING SUBTRACTION TO ADDITION

Ex 62: Convert the subtracting in addition:

$$(+4) - (+2) = (\boxed{\phantom{00}}) + (\boxed{\phantom{00}})$$

Ex 63: Convert the subtraction into addition:

$$(-5) - (-3) = (\boxed{\phantom{00}}) + (\boxed{\phantom{00}})$$

Ex 64: Convert the subtraction into addition:

$$(+4) - (-2) = (\boxed{\phantom{00}}) + (\boxed{\phantom{00}})$$

Ex 65: Convert the subtraction into addition:

$$(-1) - (+2) = (\boxed{\phantom{00}}) + (\boxed{\phantom{00}})$$

### C.2 SUBTRACTING INTEGERS STEP BY STEP

Ex 66: Calculate:

$$(+4) - (+2) = (\boxed{\phantom{00}}) + (\boxed{\phantom{00}}) = \boxed{\phantom{00}}$$

Ex 67: Calculate:

$$(-2) - (-3) = (\boxed{\phantom{00}}) + (\boxed{\phantom{00}}) = \boxed{\phantom{00}}$$

Ex 68: Calculate:

$(-4) - (+2) = (\text{ }) + (\text{ })$   
 $= \text{ }$

Ex 69: Calculate:

$(+3) - (-2) = (\text{ }) + (\text{ })$   
 $= \text{ }$

C.3 SUBTRACTING INTEGERS

Ex 70: Calculate:

$(+4) - (+2) = \text{ }$

Ex 71: Calculate:

$(-2) - (-4) = \text{ }$

Ex 72: Calculate:

$(+2) - (-3) = \text{ }$

Ex 73: Calculate:

$(-3) - (+4) = \text{ }$

C.4 SUBTRACTING INTEGERS WITHOUT EXPLICIT SIGNS

Ex 74: Calculate:

$3 - (-2) = \text{ }$

Ex 75: Calculate:

$(-2) - 3 = \text{ }$

Ex 76: Calculate:

$(-3) - (-5) = \text{ }$

Ex 77: Calculate:

$3 - 5 = \text{ }$

C.5 ADDING/SUBTRACTING MULTIPLE INTEGERS

Ex 78: Calculate:

$(+3) - (-7) - (+5) = \text{ }$

Ex 79: Calculate:

$(-2) - (-3) + (-2) = \text{ }$

Ex 80: Calculate:

$(-5) - (-4) + (-3) = \text{ }$

Ex 81: Calculate:

$(+6) - (-3) + (-4) = \text{ }$

C.6 SUBTRACTING INTEGERS IN REAL-WORLD PROBLEMS

Ex 82: In the morning, the temperature was  $-7^{\circ}\text{C}$ , and by the evening, the temperature was  $-2^{\circ}\text{C}$ . Find the variation of temperature.

$\text{ }^{\circ}\text{C}$

Ex 83: In the morning, your bank account balance was  $-50$  dollars, and by the evening, it was  $+30$  dollars. Find the change in your bank account balance.

$\text{ }$  dollars

Ex 84: A lift starts at the 5th floor and descends to the -2nd floor (below ground level). Find the change in the lift's position.

$\text{ }$  floors

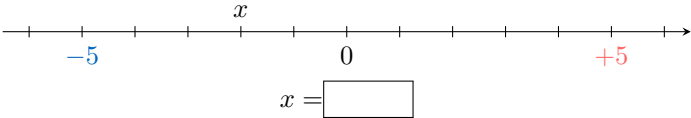
Ex 85: The GDP (Gross Domestic Product) growth rate of a country was  $-2\%$  in 2024. It was  $+3\%$  in 2025. Find the variation in the GDP growth rate.

$\text{ }\%$

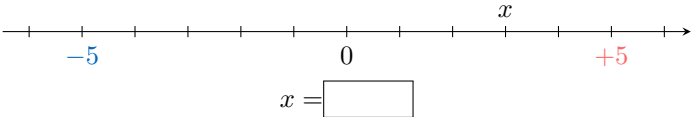
D ON THE NUMBER LINE

D.1 FINDING X ON THE NUMBER LINE

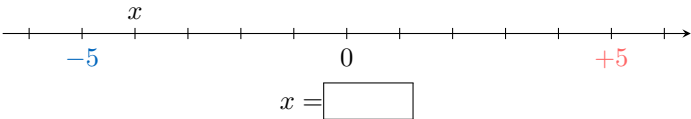
Ex 86: Find the value of  $x$ .



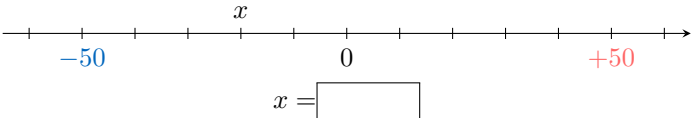
Ex 87: Find the value of  $x$ .



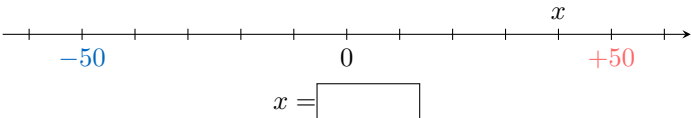
Ex 88: Find the value of  $x$ .



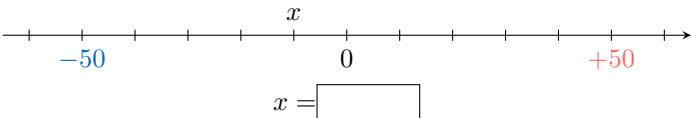
Ex 89: Find the value of  $x$ .



Ex 90: Find the value of  $x$ .

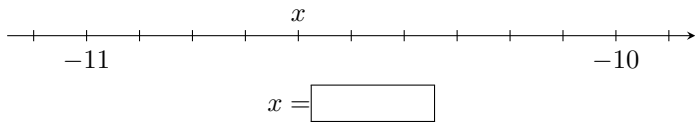


Ex 91: Find the value of  $x$ .

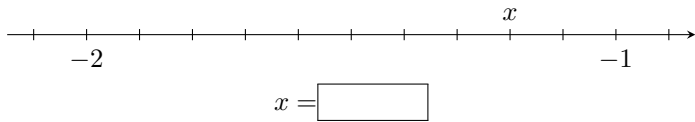


## D.2 FINDING DECIMAL NUMBERS ON THE NUMBER LINE

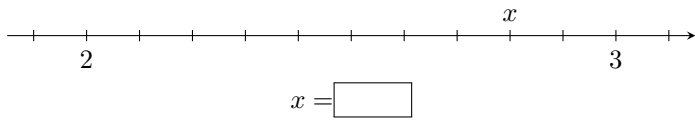
**Ex 92:** Find the value of  $x$ .



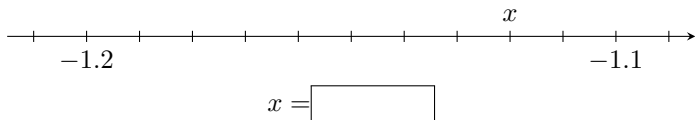
**Ex 93:** Find the value of  $x$ .



**Ex 94:** Find the value of  $x$ .



**Ex 95:** Find the value of  $x$ .



## E ORDERING

### E.1 COMPARING SMALL INTEGERS

☐ <

**Ex 96:** Compare:  $-1$  ☐  $+5$

☐ =

☐ <

**Ex 97:** Compare the numbers:  $-4$  ☐  $+3$

☐ =

☐ <

**Ex 98:** Compare the numbers:  $-2$  ☐  $-5$

☐ =

☐ <

**Ex 99:** Compare the numbers:  $+6$  ☐  $+1$

☐ =

☐ <

**Ex 100:** Compare the numbers:  $+2$  ☐  $+5$

☐ =

☐ <

**Ex 101:** Compare the numbers:  $-6$  ☐  $-1$

☐ =

☐ <

**Ex 102:** Compare the numbers:  $-1$  ☐  $+5$

☐ =

## E.2 COMPARING INTEGERS

☐ <

**Ex 103:** Compare the numbers:  $-20$  ☐  $1$

☐ =

☐ <

**Ex 104:** Compare the numbers:  $-99$  ☐  $-100$

☐ =

☐ <

**Ex 105:** Compare the numbers:  $234$  ☐  $-1200$

☐ =

☐ <

**Ex 106:** Compare the numbers:  $-18$  ☐  $-3$

☐ =

☐ <

**Ex 107:** Compare the numbers:  $230$  ☐  $200$

☐ =

☐ <

**Ex 108:** Compare the numbers:  $99$  ☐  $-100$

☐ =

## E.3 COMPARING INTEGERS IN REAL-WORLD PROBLEMS

**MCQ 109:** During a golf tournament, the scores relative to par for five different holes were:

$-2, -1, 0, +1, -3$

Order these scores from the best performance (most under par) to the worst performance (above par).

Choose one answer:

☐  $0 < +1 < -1 < -2 < -3$

☐  $-3 < -2 < -1 < 0 < +1$

☐  $+1 > 0 > -1 > -2 > -3$

☐  $-1 < -2 < -3 < 0 < +1$

**MCQ 110:** Given the depths of various lakes below sea level:

Lake	Depth below sea level
Lake Assal, Djibouti	$-155$ m
Death Valley, USA	$-86$ m
Caspian Sea, Central Asia	$-28$ m
Sea of Galilee, Israel	$-214$ m

Which lake is the deepest below sea level?

Choose one answer:

☐ Lake Assal, Djibouti

☐ Death Valley, USA

☐ Caspian Sea, Central Asia

☐ Sea of Galilee, Israel

**MCQ 111:** The recorded temperatures in a particular week were:

$-2.5^{\circ}\text{C}, 1.2^{\circ}\text{C}, -0.8^{\circ}\text{C}, 0.5^{\circ}\text{C}, -3.2^{\circ}\text{C}$

Order these temperatures from coldest to warmest.

Choose one answer:

- ☐  $1.2^{\circ}\text{C} < 0.5^{\circ}\text{C} < -0.8^{\circ}\text{C} < -2.5^{\circ}\text{C}$
- ☐  $-3.2^{\circ}\text{C} < -2.5^{\circ}\text{C} < -0.8^{\circ}\text{C} < 0.5^{\circ}\text{C} < 1.2^{\circ}\text{C}$
- ☐  $1.2^{\circ}\text{C} > 0.5^{\circ}\text{C} > -0.8^{\circ}\text{C} > -3.2^{\circ}\text{C}$
- ☐  $-0.8^{\circ}\text{C} < -2.5^{\circ}\text{C} < -3.2^{\circ}\text{C} < 0.5^{\circ}\text{C} < 1.2^{\circ}\text{C}$

**MCQ 112:** Given the years of significant events in Ancient Roman history:

Event	Year
Founding of Rome	-753
End of the Roman Republic	-27
Sacking of Rome by the Gauls	-390
Julius Caesar's assassination	-44

Which event happened the earliest?

Choose one answer:

- ☐ Founding of Rome
- ☐ End of the Roman Republic
- ☐ Sacking of Rome by the Gauls
- ☐ Julius Caesar's assassination

## F MULTIPLICATION

### F.1 MULTIPLYING SMALL INTEGERS

**Ex 113:** Calculate:

$(-2) \times (-7) = \boxed{\phantom{00}}$

**Ex 114:** Calculate:

$(-4) \times (+6) = \boxed{\phantom{00}}$

**Ex 115:** Calculate:

$(+5) \times (-3) = \boxed{\phantom{00}}$

**Ex 116:** Calculate:

$(-6) \times (-2) = \boxed{\phantom{00}}$

**Ex 117:** Calculate:

$(+3) \times (+5) = \boxed{\phantom{00}}$

**Ex 118:** Calculate:

$(-1) \times (-1) = \boxed{\phantom{00}}$

### F.2 MULTIPLYING INTEGERS WITHOUT EXPLICIT SIGNS

**Ex 119:** Calculate:

$3 \times (-2) = \boxed{\phantom{00}}$

**Ex 120:** Calculate:

$(-3) \times 8 = \boxed{\phantom{00}}$

**Ex 121:** Calculate:

$(-5) \times (-8) = \boxed{\phantom{00}}$

**Ex 122:** Calculate:

$(-6) \times 9 = \boxed{\phantom{00}}$

### F.3 CALCULATING POWERS OF NEGATIVE NUMBERS

**Ex 123:** Calculate:

$(-2)^2 = \boxed{\phantom{00}}$

**Ex 124:** Calculate:

$(-4)^2 = \boxed{\phantom{00}}$

**Ex 125:** Calculate:

$(-1)^3 = \boxed{\phantom{00}}$

**Ex 126:** Calculate:

$(-2)^3 = \boxed{\phantom{00}}$

### F.4 MULTIPLYING INTEGERS IN REAL-WORLD PROBLEMS

**Ex 127:** At midnight, the temperature was 0 degrees. The temperature continued to change by -3 degrees every hour. What was the temperature 4 hours later?

$\boxed{\phantom{00}}^{\circ}\text{C}$

**Ex 128:** A diver starts at sea level (0 meters). The diver descends 5 meters every minute. How deep is the diver after 6 minutes?

$\boxed{\phantom{00}}$  meters

**Ex 129:** A hiker is at an altitude of 150 meters. The hiker descends by 10 meters every minute. What is the hiker's altitude after 7 minutes?

$\boxed{\phantom{00}}$  meters

**Ex 130:** Your bank account has a balance of 90 euros. You make a withdrawal of 40 euros every day for 5 days. What is your account balance after 5 days?

$\boxed{\phantom{00}}$  euros



## G DIVISION

### G.1 DIVIDING SMALL INTEGERS

**Ex 131:** Calculate:

$$(+8) \div (-2) = \boxed{\phantom{00}}$$

**Ex 132:** Calculate:

$$(-12) \div (-3) = \boxed{\phantom{00}}$$

**Ex 133:** Calculate:

$$(-15) \div (+5) = \boxed{\phantom{00}}$$

**Ex 134:** Calculate:

$$(+20) \div (+4) = \boxed{\phantom{00}}$$

### G.2 DIVIDING INTEGERS WITHOUT EXPLICIT SIGNS

**Ex 135:** Calculate:

$$8 \div (-2) = \boxed{\phantom{00}}$$

**Ex 136:** Calculate:

$$-12 \div (-3) = \boxed{\phantom{00}}$$

**Ex 137:** Calculate:

$$-18 \div 6 = \boxed{\phantom{00}}$$

**Ex 138:** Calculate:

$$24 \div 4 = \boxed{\phantom{00}}$$