

# LINE EQUATIONS

## A DEFINITION

**Discover:** Consider the equation  $y = 2x - 1$ , which describes the relationship between two variables  $x$  and  $y$ . For any given value of  $x$ , we can use the equation to find the corresponding value of  $y$ . These values give coordinates  $(x, y)$  of points on the graph.

- For  $x = 1$ :

$$\begin{aligned}y &= 2 \times 1 - 1 \\ &= 1\end{aligned}$$

- For  $x = 2$ :

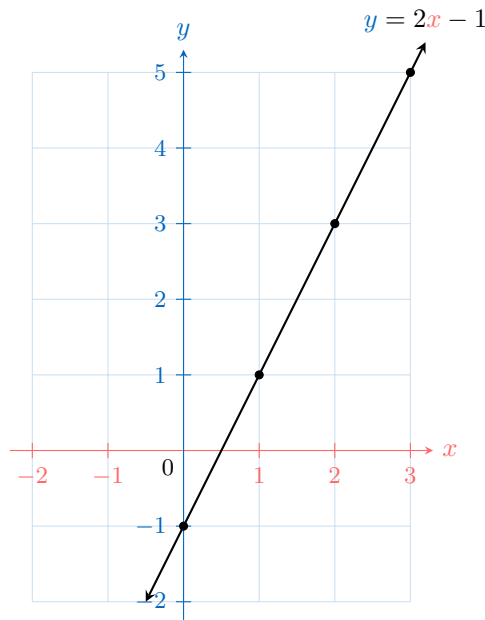
$$\begin{aligned}y &= 2 \times 2 - 1 \\ &= 3\end{aligned}$$

From calculations like these, we can construct a table of values:

|     |    |   |   |   |
|-----|----|---|---|---|
| $x$ | 0  | 1 | 2 | 3 |
| $y$ | -1 | 1 | 3 | 5 |

So, the points  $(0, -1)$ ,  $(1, 1)$ ,  $(2, 3)$ , and  $(3, 5)$  all lie on the graph.

In fact, there are infinitely many points that satisfy  $y = 2x - 1$ , forming a continuous line extending indefinitely in both directions (indicated with arrowheads).



$y = 2x - 1$  is an equation that relates  $x$  and  $y$  for all points on the line.

### Definition Equation of a line

The **equation of a line** can be written as:

$$y = mx + c$$

where  $m$  is the **slope** and  $c$  is the **y-intercept**.

**Ex:**

