PROPERTIES OF INTEGERS

A NUMBERS 1 AND 0

A.1 APPLYING NUMBER PROPERTIES

Ex 1: Calculate the following expression without using a calculator:

$$(4 \times 22 + 3 + 22 \div 2) \times 0 =$$

Ex 2: Consider the following sequence of algebraic manipulations:

$$0 \times 2 = 0$$
 Line 1
 $2 = \frac{0}{0}$ Line 2 (dividing by 0)
 $2 = \frac{1 \times \emptyset}{1 \times \emptyset}$ Line 3 (cancelling common factor)
 $2 = 1$ Line 4

This sequence appears to show that 2=1, which is a false result. Identify the line where an invalid mathematical operation is performed.

The error occurs in Line

Ex 3: Calculate the following expression without using a calculator:

$$2 + (120 - 45) \times (200 - 200) =$$

Ex 4: Calculate the following expression without using a calculator:

$$(15 + 3 \times 5 - 30) \times (100 \times 11) =$$

B DIVISION WITH REMAINDERS

B.1 CALCULATING THE DIVISION WITH REMAINDERS

Ex 5: Write the division with remainder of 21 by 5:

$$21 = 5 \times \boxed{ } + \boxed{ }$$

Ex 6: Write the division with remainder of 37 by 3:

$$37 = 3 \times$$

Ex 7: Write the division with remainder of 63 by 4:

$$63 = 4 \times \boxed{+}$$

Ex 8: Write the division with remainder of 154 by 6:

$$154 = 6 \times \boxed{} + \boxed{}$$

Ex 9: Write the division with remainder of 632 by 5:

$$632 = 5 \times \boxed{ } + \boxed{ }$$

B.2 SOLVING REAL-WORLD PROBLEMS

Ex 10: A farmer shares 243 eggs into boxes such that each box contains 6 eggs.

How many boxes are needed?

	_
	boxes
	002101

How many eggs remain without being placed in a box?



Ex 11: A farmer's inheritance of 123 sheep is to be divided equally among 4 children.

How many sheep does each child receive?



How many sheep remain undistributed?



Ex 12: A gardener arranges 200 roses into bouquets such that each bouquet contains 12 roses.

How many bouquets are needed?



How many roses remain without being placed in a bouquet?



 \mathbf{Ex} 13: A child entering middle school decides to give his 300 marbles to his 7 cousins.

How many marbles does each cousin receive?



How many marbles remain undistributed?

	l marble
	manne

Ex 14: A coach organizes 37 soccer players into teams such that each team contains 5 players. The remaining players are substitutes.

How many full teams can be formed?



How many players are substitutes?

playe	21
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C DIVISIBILITY

C.1 DETERMINING DIVISIBILITY

MCQ 15: Is 10 divisible by 5?

- ☐ Yes
- □ No

MCQ 16: Is 82 divisible by 4?	$\Box \ 45 = 5 \times 9$
□ Yes	MCQ 26: List all the factors of 6.
□ No	Choose 1 answer: $\Box 1, 2, 3, 4, 6$
MCQ 17: Is 72 divisible by 5?	$\Box 1, 2, 3, 6$
□ Yes	$\Box 1, 2, 3, 6, 12$
□ No	MCQ 27: List all the factors of 24.
MCQ 18: Is 234 divisible by 3?	Choose 1 answer: $\Box 1, 2, 3, 4, 6, 8, 12, 24$
□ Yes	$\Box 1, 2, 3, 4, 6, 8$
□ No	$\Box 1, 2, 3, 4, 5, 6, 8, 12, 24$
C.2 DETERMINING MULTIPLICITY	MCQ 28: List all the factors of 40. Choose 1 answer:
MCQ 19: Is 73 a multiple of 9?	$\Box 1, 2, 4, 5, 8, 10, 40$
□ Yes	$\square \ 1, 2, 4, 5, 8, 10, 12, 20, 40$
□ No	$\Box 1, 2, 4, 5, 8, 10, 20, 40$
MCQ 20: Is 77 a multiple of 11?	D DIVISIBILITY CRITERIA
□ Yes	D.1 DETERMINING DIVISIBILITY FOR 2 AND 5
□ No	MCQ 29: Is 98 divisible by 2?
MCQ 21: Is 50 a multiple of 4?	□ Yes
□ Yes	□ No
□ No	MCQ 30: Is 315 divisible by 2?
MCQ 22: Is 100 a multiple of 12?	□ Yes □ No
□ Yes	MCQ 31: Is 462 divisible by 2?
□ No	☐ Yes
C.3 DETERMINING FACTORS	\square No
MCQ 23: Is 10 a factor of 60?	MCQ 32: Is 799 divisible by 2?
□ Yes	☐ Yes
□ No	□ No
MCQ 24: Which of the following numbers are factors of 64?	MCQ 33: Is 45 divisible by 5? ☐ Yes
Choose all answers that apply:	□ No
\square 2	MCQ 34: Is 80 divisible by 5?
\Box 4	☐ Yes
	□ No
\square 32	MCQ 35: Is 126 divisible by 5?
MCQ 25: Which equation shows that 5 is a factor of 45? Choose 1 answer:	□ Yes □ No
$\Box \ 45 = 5 + 40$	MCQ 36: Is 301 divisible by 5?
$\Box \ 45 = 50 - 5$	☐ Yes
$ 45 = 225 \div 5$	□ No

D.2 DETERMINING DIVISIBILITY FOR 3 AND 9	
MCQ 37: Is 162 divisible by 3?	□ No
□ Yes	MCQ 49: Is 179 divisible by 4? ☐ Yes
□ No	□ No
MCQ 38: Is 305 divisible by 3?	
□ Yes	MCQ 50: Is 520 divisible by 4?
□ No	□ Yes □ No
MCQ 39: Is 888 divisible by 3?	
□ Yes	MCQ 51: Is 567 divisible by 4?
□ No	□ Yes □ No
MCQ 40: Is 504 divisible by 3?	□ No
Yes	E PRIME NUMBER
□ No	E.1 CHECKING IF PRIME
MCQ 41: Is 126 divisible by 9?	MCQ 52: State whether 6 is a prime number.
□ Yes	□ Yes
□ No	□ No
MCQ 42: Is 235 divisible by 9?	MCQ 53: State whether 5 is a prime number.
□ Yes	☐ Yes
□ No	□ No
MCQ 43: Is 369 divisible by 9?	MCQ 54: State whether 9 is a prime number.
Yes	□ Yes
□ No	□ No
	MCQ 55: State whether 7 is a prime number.
MCQ 44: Is 441 divisible by 9?	□ Yes
□ Yes □ No	□ No
	MCQ 56: State whether 12 is a prime number.
D.3 DETERMINING DIVISIBILITY FOR 4	□ Yes
MCQ 45: Is 188 divisible by 4?	□ No
□ Yes	MCQ 57: State whether 10 is a prime number.
□ No	□ Yes
MCQ 46: Is 373 divisible by 4?	□ No
□ Yes	MCQ 58: State whether 13 is a prime number.
\square No	□ Yes
MCQ 47: Is 412 divisible by 4?	□ No
□ Yes	MCQ 59: State whether 11 is a prime number.
□ No	□ Yes
MCQ 48: Is 256 divisible by 4?	\square No

F PRIME FACTORIZATION

F.1 WRITING IN PRIME FACTORS: LEVEL 1

Ex 60: Write the number as a product of prime factors :

 \mathbf{Ex} 61: Write the number as a product of prime factors :

 $\mathbf{Ex}\ \mathbf{62:}\ \mathbf{Write}\ \mathbf{the}\ \mathbf{number}\ \mathbf{as}\ \mathbf{a}\ \mathbf{product}\ \mathbf{of}\ \mathbf{prime}\ \mathbf{factors}:$

 \mathbf{Ex} 63: Write the number as a product of prime factors :

F.2 WRITING IN PRIME FACTORS: LEVEL 2

 $\mathbf{Ex}\ \mathbf{64:}\ \mathbf{Write}\ \mathbf{the}\ \mathbf{number}\ \mathbf{as}\ \mathbf{a}\ \mathbf{product}\ \mathbf{of}\ \mathbf{prime}\ \mathbf{factors}:$

 $\mathbf{Ex}\ \mathbf{65}\text{:}\ \mathbf{Write}\ \mathbf{the}\ \mathbf{number}\ \mathbf{as}\ \mathbf{a}\ \mathbf{product}\ \mathbf{of}\ \mathbf{prime}\ \mathbf{factors}:$

Ex 66: Write the number as a product of prime factors :

 \mathbf{Ex} 67: Write the number as a product of prime factors :

F.3 WRITING IN PRIME FACTORS: LEVEL 3

Ex 68: Write the number as a product of prime factors:

Ex 69: Write the number as a product of prime factors :

 $\mathbf{Ex}\ \mathbf{70:}\ \mathbf{Write}\ \mathbf{the}\ \mathbf{number}\ \mathbf{as}\ \mathbf{a}\ \mathbf{product}\ \mathbf{of}\ \mathbf{prime}\ \mathbf{factors}:$

 \mathbf{Ex} 71: Write the number as a product of prime factors :