SEQUENCES

A NUMERICAL SEQUENCE

A.1 FINDING u_n

Ex 1:

n	1	2	3	4	5	6
u_n	3	5	7	9	11	13

What is u_4 ?



Ex 2:

	-	_	_			
n	1	2	3	4	5	6
u_n	2	6	12	20	30	42

What is u_5 ?



Ex 3:

n	1	2	3	4	5	6	7	8
$\overline{u_n}$	4	9	16	25	36	49	64	81

What is u_7 ?



Ex 4:

n	1	2	3	4	5	6	7	8
u_n	1	3	7	15	31	63	127	255

What is u_8 ?



A.2 FINDING u_n IN AN ARITHMETIC SEQUENCE

Ex 5: What is u_6 for this sequence?

\overline{n}	1	2	3	4	5	6
u_n	3	5	7	9	11	

Ex 6: What is u_6 for this sequence?

\overline{n}	1	2	3	4	5	6
u_n	3	8	13	18	23	

Ex 7: What is u_5 for this sequence?

n	1	2	3	4	5
u_m	20	18	16	14	

Ex 8: What is u_6 for this sequence?

n	1	2	3	4	5	6
u_n	80	70	60	50	40	

B DEFINITION USING A RECURSIVE RULE

B.1 CALCULATING THE FIRST TERMS

Ex 9: Write the sequence defined by: the first term is 7, and each term is obtained by adding 4 to the previous term.

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Ex 10: Write the sequence defined by: the first term is 1, and each term is obtained by multiplying the previous term by 2.

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Ex 11: Write the sequence defined by: the first term is 10, and each term is obtained by subtracting 5 from the previous term.

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Ex 12: Write the sequence defined by: the first term is 2.5, and each term is obtained by adding 0.5 to the previous term.

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B.2 IDENTIFYING THE RECURSIVE RULE

Ex 13: Given the sequence: (3, 5, 7, 9, 11, 13, ...)

• The first term is	
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 \square Add

• The rule is
$$\Box$$
 Subtract \Box Multiply

☐ Divide

Ex 14: Given the sequence: (60, 55, 50, 45, 40, 35, ...)

•	The	first	$_{\rm term}$	is	١.

 \square Add

□ Divide

Ex 15: Given the sequence: (64, 32, 16, 8, 4, 2, ...)

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•	The	first	$_{\rm term}$	is	

 \square Add

Ex 16: Given the sequence: (1, 10, 100, 1000, 10000,...)

•	The	first	term	is	
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 \square Add

_	The mule is	\square Subtract	
•	The rule is	\Box Multiply	
		□ Divide	

B.3 IDENTIFYING THE RECURSIVE RULE IN GEOMETRIC PATTERNS

Ex 17:	Observe	the	following	pattern	made	with	sticks:
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Fill in the table below:

Diagram number	1	2	3	4
Number of sticks				

What rule can you find for the number of sticks?

Start with sticks. Add sticks for the next diagram.

Ex 18: Observe the following pattern made with sticks:



Fill in the table below:

Diagram number	1	2	3	4
Number of sticks				

What rule can you find for the number of sticks?

Start with sticks. Add sticks for the next diagram.

Ex 19: Observe the following pattern made with sticks:



Fill in the table below:

Diagram number	1	2	3	4
Number of sticks				

What rule can you find for the number of sticks?

Start with sticks. Add sticks for the next diagram.

Ex 20: Observe the following pattern made with sticks:



Fill in the table below:

Diagram number	1	2	3	4
Number of sticks				

What rule can you find for the number of sticks?

Start with sticks. Add sticks for the next diagram.

B.4 MODELING REAL SITUATIONS WITH SEQUENCES

Ex 21: \square A scientist observes a culture of bacteria. At the start, there are $u_0 = 5$ bacteria in a petri dish. Each day, the number of bacteria doubles.

Let u_n be the number of bacteria at the day n. What are the first five terms of the sequence (u_n) ?

- $u_1 =$ bacteria
- $u_2 =$ bacteria
- $u_3 =$ bacteria
- $u_4 =$ bacteria
- $u_5 =$ bacteria

Ex 22: Let u_n be the number of steps I have walked at the end of day n. On day 0, I walk $u_0 = 1000$ steps. Each day, I walk 500 more steps than the previous day.

What are the first terms of the sequence (u_n) ?

- $u_1 =$ steps
- $u_2 = |$ steps
- $u_3 = \boxed{}$ steps
- $u_4 = |$ steps
- $u_5 = |$ steps

Ex 23: Suppose I deposit \$100 in a savings account. Each year, my amount is multiplied by 1.1 (that is, it increases by 10% every year).

Let u_n be the amount of money in the account after n years. What are the first five terms of the sequence (u_n) ?

- $u_0 = \boxed{ dollars}$
- $u_1 = |$ dollars
- $u_2 = \boxed{ dollars}$
- $u_3 = |$ dollars
- $u_4 = |$ dollars

Ex 24: Let u_n be the amount of money I have at the beginning of week n. At the start, I have $u_0 = 20$ dollars. At the end of each week, my parents give me \$ 10 more.

What are the first terms of the sequence (u_n) ?

- $u_1 =$ dollars
- $u_2 = |$ dollars
- $u_3 = \boxed{ }$ dollars
- $u_4 = |$ dollars
- $u_5 = |$ dollars

C DEFINITION USING AN EXPLICIT RULE

C.1 CALCULATING TERMS FROM AN EXPLICIT FORMULA

Ex 25: Consider the sequence defined by the explicit formula: $u_n = 3n + 2$.

Write the first four terms of this sequence.

- $u_0 =$
- $u_1 =$
- $u_2 =$
- $u_3 = \boxed{}$

Ex 26: Consider the sequence defined by the explicit formula: $u_n = -10n + 100$.

Write the first four terms of this sequence.

- $u_0 =$
- $u_1 =$
- $u_2 =$
- $u_3 =$

Ex 27: Consider the sequence defined by the explicit formula: $u_n = n^2 + 2$.

Write the first four terms of this sequence.

- $u_0 =$
- $u_1 =$
- $u_2 =$
- $u_3 =$

Ex 28: Consider the sequence defined by the explicit formula: $u_n = (n+1)n$.

Write the first four terms of this sequence.

- $u_0 =$
- $u_1 =$
- $u_2 =$
- $u_3 =$

C.2 MODELING REAL SITUATIONS WITH SEQUENCES

Ex 29: You start with \$30 and each week your parent gives you \$10

The amount of money you have after n weeks is given by the formula:

 $u_n = \text{Initial Amount} + \text{Nbr weeks} \times \text{Amount received each week}$

- $= 30 + n \times 10$
- = 30 + 10n

where u_n is the amount after n weeks. How much money will you have after 20 weeks?

dollars

Ex 30: You deposit \$1 500 in a savings account that pays simple interest at a rate of 4% per year.

The amount of money in your account after n years is given by the formula:

 $u_n = \text{Initial Amount} + \text{Nbr years} \times \text{Percentage of the initial amount}$

- $= 1500 + n \times 0.04 \times 1500$
- = 1500 + 60n

where u_n is the amount after n years. What is your amount at year 20?

dollars

Ex 31: You start a stamp collection with 12 stamps. Each month, you add 4 new stamps to your collection.

The number of stamps you have after n months is given by the formula:

 $u_n = \text{Initial number of stamps} + \text{Nbr months} \times \text{Stamps added per stamps}$

- $=12+n\times4$
- = 12 + 4n

where u_n is the number of stamps after n months. How many stamps will you have after 15 months?

stamps

Ex 32: A school plants 5 trees in its garden to start. Every year, they plant 3 new trees.

The total number of trees after n years is given by the formula:

 $u_n = \text{Initial number of trees} + \text{Nbr years} \times \text{Trees planted per year}$

- $=5+n\times 3$
- = 5 + 3n

where u_n is the number of trees after n years. How many trees will there be after 12 years?

trees