

# SOLVING EQUATIONS

## A DEFINITIONS

### A.1 MATH ESCAPE ROOM: LEVEL 1

**MCQ 1:** For this Math escape room, the code is:

$$\bigcirc + 5 = 9$$

Which code do you use to enter?

- ☐  $\bigcirc = 2$
- ☒  $\bigcirc = 4$
- ☐  $\bigcirc = 5$
- ☐  $\bigcirc = 9$

Answer:

- For  $\bigcirc = 2$ :  
 $(2) + 5 = 9$   
 $7 = 9$  (False)
- For  $\bigcirc = 4$ :  
 $(4) + 5 = 9$   
 $9 = 9$  (True)
- For  $\bigcirc = 5$ :  
 $(5) + 5 = 9$   
 $10 = 9$  (False)
- For  $\bigcirc = 9$ :  
 $(9) + 5 = 9$   
 $14 = 9$  (False)

Therefore, the correct code to enter is  $\bigcirc = 4$ .

**MCQ 2:** For this Math escape room, the code is:

$$\triangle + 10 = 1 + 2 \times 6$$

Which code do you use to enter?

- ☒  $\triangle = 3$
- ☐  $\triangle = 5$
- ☐  $\triangle = 8$
- ☐  $\triangle = 10$

Answer:

- For  $\triangle = 3$ :  
 $(3) + 10 = 1 + 2 \times 6$   
 $13 = 1 + 12$   
 $13 = 13$  (True)
- For  $\triangle = 5$ :  
 $(5) + 10 = 1 + 2 \times 6$   
 $15 = 1 + 12$   
 $15 = 13$  (False)

- For  $\triangle = 8$ :

$$\begin{aligned}(8) + 10 &= 1 + 2 \times 6 \\ 18 &= 1 + 12 \\ 18 &= 13 \quad (\text{False})\end{aligned}$$

- For  $\triangle = 10$ :

$$\begin{aligned}(10) + 10 &= 1 + 2 \times 6 \\ 20 &= 1 + 12 \\ 20 &= 13 \quad (\text{False})\end{aligned}$$

Therefore, the correct code to enter is  $\triangle = 3$ .

**MCQ 3:** For this Math escape room, the code is:

$$\square + 5 = 2 \times 4 + 1$$

Which code do you use to enter?

- ☐  $\square = 6$
- ☐  $\square = 8$
- ☐  $\square = 5$
- ☒  $\square = 4$

Answer:

- For  $\square = 6$ :  
 $(6) + 5 = 2 \times 4 + 1$   
 $11 = 8 + 1$   
 $11 = 9$  (False)
- For  $\square = 8$ :  
 $(8) + 5 = 2 \times 4 + 1$   
 $13 = 8 + 1$   
 $13 = 9$  (False)
- For  $\square = 5$ :  
 $(5) + 5 = 2 \times 4 + 1$   
 $10 = 8 + 1$   
 $10 = 9$  (False)
- For  $\square = 4$ :  
 $(4) + 5 = 2 \times 4 + 1$   
 $9 = 8 + 1$   
 $9 = 9$  (True)

Therefore, the correct code to enter is  $\square = 4$ .

**MCQ 4:** For this Math escape room, the code is:

$$\bigcirc - 4 = 3 \times 2 - 1$$

Which code do you use to enter?

- ☐  $\bigcirc = 7$
- ☐  $\bigcirc = 6$

$$\square \bigcirc = 5$$

$$\boxtimes \bigcirc = 9$$

Answer:

- For  $\bigcirc = 7$ :

$$\begin{aligned}(7) - 4 &= 3 \times 2 - 1 \\ 3 &= 6 - 1 \\ 3 &= 5 \quad (\text{False})\end{aligned}$$

- For  $\bigcirc = 6$ :

$$\begin{aligned}(6) - 4 &= 3 \times 2 - 1 \\ 2 &= 6 - 1 \\ 2 &= 5 \quad (\text{False})\end{aligned}$$

- For  $\bigcirc = 5$ :

$$\begin{aligned}(5) - 4 &= 3 \times 2 - 1 \\ 1 &= 6 - 1 \\ 1 &= 5 \quad (\text{False})\end{aligned}$$

- For  $\bigcirc = 9$ :

$$\begin{aligned}(9) - 4 &= 3 \times 2 - 1 \\ 5 &= 6 - 1 \\ 5 &= 5 \quad (\text{True})\end{aligned}$$

Therefore, the correct code to enter is  $\bigcirc = 9$ .

## A.2 MATH ESCAPE ROOM: LEVEL 2

**MCQ 5:** For this Math escape room, the code is:

$$2 \times \bigcirc - 2 = \bigcirc + 10$$

Which code do you use to enter?

- ☐  $\bigcirc = 8$
- ☐  $\bigcirc = 10$
- ☒  $\bigcirc = 12$
- ☐  $\bigcirc = 14$

Answer:

- For  $\bigcirc = 8$ :

$$\begin{aligned}2 \times (8) - 2 &= (8) + 10 \\ 16 - 2 &= 8 + 10 \\ 14 &= 18 \quad (\text{False})\end{aligned}$$

- For  $\bigcirc = 10$ :

$$\begin{aligned}2 \times (10) - 2 &= (10) + 10 \\ 20 - 2 &= 10 + 10 \\ 18 &= 20 \quad (\text{False})\end{aligned}$$

- For  $\bigcirc = 12$ :

$$\begin{aligned}2 \times (12) - 2 &= (12) + 10 \\ 24 - 2 &= 12 + 10 \\ 22 &= 22 \quad (\text{True})\end{aligned}$$

- For  $\bigcirc = 14$ :

$$\begin{aligned}2 \times (14) - 2 &= (14) + 10 \\ 28 - 2 &= 14 + 10 \\ 26 &= 24 \quad (\text{False})\end{aligned}$$

Therefore, the correct code to enter is  $\bigcirc = 12$ .

**MCQ 6:** For this Math escape room, the code is:

$$3x + 7 = x + 19$$

Which code do you use to enter?

- ☐  $x = 2$
- ☐  $x = 4$
- ☒  $x = 6$
- ☐  $x = 8$

Answer:

- For  $x = 2$ :

$$\begin{aligned}3 \times (2) + 7 &= (2) + 19 \\ 6 + 7 &= 2 + 19 \\ 13 &= 21 \quad (\text{False})\end{aligned}$$

- For  $x = 4$ :

$$\begin{aligned}3 \times (4) + 7 &= (4) + 19 \\ 12 + 7 &= 4 + 19 \\ 19 &= 23 \quad (\text{False})\end{aligned}$$

- For  $x = 6$ :

$$\begin{aligned}3 \times (6) + 7 &= (6) + 19 \\ 18 + 7 &= 6 + 19 \\ 25 &= 25 \quad (\text{True})\end{aligned}$$

- For  $x = 8$ :

$$\begin{aligned}3 \times (8) + 7 &= (8) + 19 \\ 24 + 7 &= 8 + 19 \\ 31 &= 27 \quad (\text{False})\end{aligned}$$

Therefore, the correct code to enter is  $x = 6$ .

**MCQ 7:** For this Math escape room, the code is:

$$2x - 2 = x + 10$$

Which code do you use to enter?

- ☐  $x = 6$
- ☐  $x = 8$
- ☐  $x = 10$
- ☒  $x = 12$

Answer:

- For  $x = 6$ :

$$\begin{aligned}2 \times (6) - 2 &= (6) + 10 \\ 12 - 2 &= 6 + 10 \\ 10 &= 16 \quad (\text{False})\end{aligned}$$

- For  $x = 8$ :

$$2 \times (8) - 2 = (8) + 10$$

$$16 - 2 = 8 + 10$$

$$14 = 18 \quad (\text{False})$$

- For  $x = 10$ :

$$2 \times (10) - 2 = (10) + 10$$

$$20 - 2 = 10 + 10$$

$$18 = 20 \quad (\text{False})$$

- For  $x = 12$ :

$$2 \times (12) - 2 = (12) + 10$$

$$24 - 2 = 12 + 10$$

$$22 = 22 \quad (\text{True})$$

Therefore, the correct code to enter is  $x = 12$ .

**MCQ 8:** For this Math escape room, the code is:

$$x \times (x - 2) = 24$$

Which code do you use to enter?

☒  $x = 6$

☐  $x = 7$

☐  $x = 8$

☐  $x = 9$

Answer:

- For  $x = 6$ :

$$(6) \times ((6) - 2) = 24$$

$$6 \times 4 = 24$$

$$24 = 24 \quad (\text{True})$$

- For  $x = 7$ :

$$(7) \times ((7) - 2) = 24$$

$$7 \times 5 = 24$$

$$35 = 24 \quad (\text{False})$$

- For  $x = 8$ :

$$(8) \times ((8) - 2) = 24$$

$$8 \times 6 = 24$$

$$48 = 24 \quad (\text{False})$$

- For  $x = 9$ :

$$(9) \times ((9) - 2) = 24$$

$$9 \times 7 = 24$$

$$63 = 24 \quad (\text{False})$$

Therefore, the correct code to enter is  $x = 6$ .

### A.3 MATH ESCAPE ROOM: LEVEL 3

**MCQ 9:** For this Math escape room, the code is:

$$x^2 - 4 = 0$$

Which code do you use to enter?

☒  $x = 2$

☐  $x = 3$

☐  $x = 4$

☐  $x = 5$

Answer:

- For  $x = 2$ :

$$(2)^2 - 4 = 0$$

$$4 - 4 = 0$$

$$0 = 0 \quad (\text{True})$$

- For  $x = 3$ :

$$(3)^2 - 4 = 0$$

$$9 - 4 = 0$$

$$5 = 0 \quad (\text{False})$$

- For  $x = 4$ :

$$(4)^2 - 4 = 0$$

$$16 - 4 = 0$$

$$12 = 0 \quad (\text{False})$$

- For  $x = 5$ :

$$(5)^2 - 4 = 0$$

$$25 - 4 = 0$$

$$21 = 0 \quad (\text{False})$$

Therefore, the correct code to enter is  $x = 2$ .

**MCQ 10:** For this Math escape room, the code is:

$$x^2 - 2x + 1 = 0$$

Which code do you use to enter?

☒  $x = 0$

☐  $x = 1$

☐  $x = 2$

☐  $x = 3$

Answer:

- For  $x = 0$ :

$$(0)^2 - 2 \times (0) + 1 = 0$$

$$0 - 0 + 1 = 0$$

$$1 = 0 \quad (\text{False})$$

- For  $x = 1$ :

$$(1)^2 - 2 \times (1) + 1 = 0$$

$$1 - 2 + 1 = 0$$

$$0 = 0 \quad (\text{True})$$

- For  $x = 2$ :

$$\begin{aligned} (2)^2 - 2 \times (2) + 1 &= 0 \\ 4 - 4 + 1 &= 0 \\ 1 &= 0 \quad (\text{False}) \end{aligned}$$

- For  $x = 3$ :

$$\begin{aligned} (3)^2 - 2 \times (3) + 1 &= 0 \\ 9 - 6 + 1 &= 0 \\ 4 &= 0 \quad (\text{False}) \end{aligned}$$

Therefore, the correct code to enter is  $x = 1$ .

**MCQ 11:** For this Math escape room, the code is:

$$\frac{2x+1}{x-1} = 3$$

Which code do you use to enter?

- ☐  $x = 2$
- ☐  $x = 3$
- ☒  $x = 4$
- ☐  $x = 5$

Answer:

- For  $x = 2$ :

$$\begin{aligned} \frac{2 \times (2) + 1}{(2) - 1} &= 3 \\ \frac{4 + 1}{2 - 1} &= 3 \\ \frac{5}{1} &= 3 \\ 5 &= 3 \quad (\text{False}) \end{aligned}$$

- For  $x = 3$ :

$$\begin{aligned} \frac{2 \times (3) + 1}{(3) - 1} &= 3 \\ \frac{6 + 1}{3 - 1} &= 3 \\ \frac{7}{2} &= 3 \\ 3.5 &= 3 \quad (\text{False}) \end{aligned}$$

- For  $x = 4$ :

$$\begin{aligned} \frac{2 \times (4) + 1}{(4) - 1} &= 3 \\ \frac{8 + 1}{4 - 1} &= 3 \\ \frac{9}{3} &= 3 \\ 3 &= 3 \quad (\text{True}) \end{aligned}$$

- For  $x = 5$ :

$$\begin{aligned} \frac{2 \times (5) + 1}{(5) - 1} &= 3 \\ \frac{10 + 1}{5 - 1} &= 3 \\ \frac{11}{4} &= 3 \\ 2.75 &= 3 \quad (\text{False}) \end{aligned}$$

Therefore, the correct code to enter is  $x = 4$ .

## B SOLVING BY TRIAL AND ERROR

### B.1 FINDING A SOLUTION: LEVEL 1

**Ex 12:** Consider the equation  $2x + 3 = 11$ .

Use the trial-and-error method to find a solution (try  $x = 2, 3, \dots$ ).

$$x = \boxed{4}$$

Answer:

- Try  $x = 2$ :

$$\begin{aligned} 2 \times (2) + 3 &= 11 \\ 4 + 3 &= 11 \\ 7 &= 11 \quad (\text{False}) \end{aligned}$$

- Try  $x = 3$ :

$$\begin{aligned} 2 \times (3) + 3 &= 11 \\ 6 + 3 &= 11 \\ 9 &= 11 \quad (\text{False}) \end{aligned}$$

- Try  $x = 4$ :

$$\begin{aligned} 2 \times (4) + 3 &= 11 \\ 8 + 3 &= 11 \\ 11 &= 11 \quad (\text{True}) \end{aligned}$$

Therefore, a solution to the equation  $2x + 3 = 11$  is  $x = 4$ .

**Ex 13:** Consider the equation  $3x - 5 = 10$ .

Use the trial-and-error method to find a solution (try  $x = 4, 5, \dots$ ).

$$x = \boxed{5}$$

Answer:

- Try  $x = 4$ :

$$\begin{aligned} 3 \times (4) - 5 &= 10 \\ 12 - 5 &= 10 \\ 7 &= 10 \quad (\text{False}) \end{aligned}$$

- Try  $x = 5$ :

$$\begin{aligned} 3 \times (5) - 5 &= 10 \\ 15 - 5 &= 10 \\ 10 &= 10 \quad (\text{True}) \end{aligned}$$

Therefore, a solution to the equation  $3x - 5 = 10$  is  $x = 5$ .

**Ex 14:** Consider the equation  $x(x - 1) = 6$ .

Use the trial-and-error method to find a solution (try  $x = 2, 3, \dots$ ).

$$x = \boxed{3}$$

Answer:

- Try  $x = 2$ :

$$\begin{aligned} (2) \times ((2) - 1) &= 6 \\ 2 \times 1 &= 6 \\ 2 &= 6 \quad (\text{False}) \end{aligned}$$

- Try  $x = 3$ :

$$\begin{aligned} (3) \times ((3) - 1) &= 6 \\ 3 \times 2 &= 6 \\ 6 &= 6 \quad (\text{True}) \end{aligned}$$

Therefore, a solution to the equation  $x(x-1) = 6$  is  $x = 3$ .

**Ex 15:** Consider the equation  $2x - 3 = 5x - 9$ .

Use the trial-and-error method to find a solution (try  $x = 0, 1, \dots$ ).

$$x = \boxed{2}$$

Answer:

- Try  $x = 0$ :

$$\begin{aligned} 2 \times (0) - 3 &= 5 \times (0) - 9 \\ 0 - 3 &= 0 - 9 \\ -3 &= -9 \quad (\text{False}) \end{aligned}$$

- Try  $x = 1$ :

$$\begin{aligned} 2 \times (1) - 3 &= 5 \times (1) - 9 \\ 2 - 3 &= 5 - 9 \\ -1 &= -4 \quad (\text{False}) \end{aligned}$$

- Try  $x = 2$ :

$$\begin{aligned} 2 \times (2) - 3 &= 5 \times (2) - 9 \\ 4 - 3 &= 10 - 9 \\ 1 &= 1 \quad (\text{True}) \end{aligned}$$

Therefore, a solution to the equation  $2x - 3 = 5x - 9$  is  $x = 2$ .

## B.2 FINDING A SOLUTION: LEVEL 2

**Ex 16:** Consider the equation  $x^2 - 2x + 1 = 0$ .

Use the trial-and-error method to find a solution (try  $x = 0, 1, \dots$ ).

$$x = \boxed{1}$$

Answer:

- Try  $x = 0$ :

$$\begin{aligned} (0)^2 - 2 \times (0) + 1 &= 0 \\ 0 - 0 + 1 &= 0 \\ 1 &= 0 \quad (\text{False}) \end{aligned}$$

- Try  $x = 1$ :

$$\begin{aligned} (1)^2 - 2 \times (1) + 1 &= 0 \\ 1 - 2 + 1 &= 0 \\ 0 &= 0 \quad (\text{True}) \end{aligned}$$

Therefore, a solution to the equation  $x^2 - 2x + 1 = 0$  is  $x = 1$ .

**Ex 17:** Consider the equation  $x^2 - 9 = 0$ .

Use the trial-and-error method to find a solution (try  $x = 2, 3, \dots$ ).

$$x = \boxed{3}$$

Answer:

- Try  $x = 2$ :

$$\begin{aligned} (2)^2 - 9 &= 0 \\ 4 - 9 &= 0 \\ -5 &= 0 \quad (\text{False}) \end{aligned}$$

- Try  $x = 3$ :

$$\begin{aligned} (3)^2 - 9 &= 0 \\ 9 - 9 &= 0 \\ 0 &= 0 \quad (\text{True}) \end{aligned}$$

Therefore, a solution to the equation  $x^2 - 9 = 0$  is  $x = 3$ .

**Ex 18:** Consider the equation  $\frac{x+2}{x-2} = 2$ .

Use the trial-and-error method to find a solution (try  $x = 6, 3, 4$ ).

$$x = \boxed{6}$$

Answer:

- Try  $x = 6$ :

$$\begin{aligned} \frac{6+2}{6-2} &= 2 \\ \frac{8}{4} &= 2 \\ 2 &= 2 \quad (\text{True}) \end{aligned}$$

- Try  $x = 3$ :

$$\begin{aligned} \frac{3+2}{3-2} &= 2 \\ \frac{5}{1} &= 2 \\ 5 &= 2 \quad (\text{False}) \end{aligned}$$

- Try  $x = 4$ :

$$\begin{aligned} \frac{4+2}{4-2} &= 2 \\ \frac{6}{2} &= 2 \\ 3 &= 2 \quad (\text{False}) \end{aligned}$$

Therefore, a solution to the equation  $\frac{x+2}{x-2} = 2$  is  $x = 6$ .

## C EQUIVALENT EQUATIONS

### C.1 SOLVING EQUATIONS BY ADDING OR SUBTRACTING

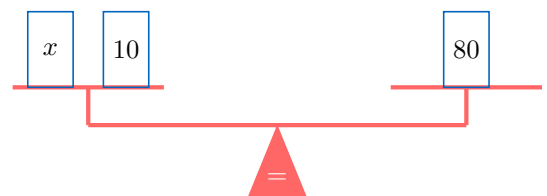
**Ex 19:** Solve for  $x$ :

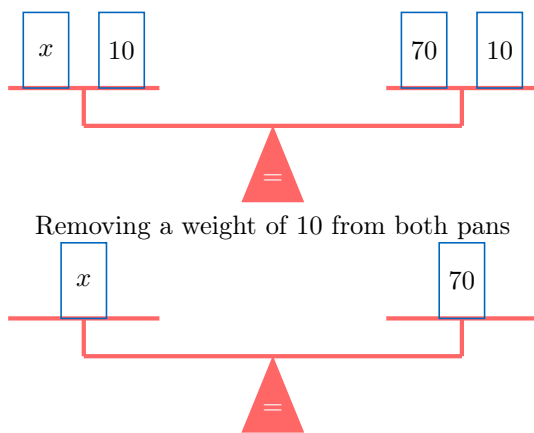
$$x + 10 = 80$$

$$x = \boxed{70}$$

Answer:

- Balance scale:





- Equivalent equations:

$$\begin{aligned}
 x + 10 &= 80 \\
 x + 10 - 10 &= 80 - 10 & (-10) \\
 x + 0 &= 70 \\
 x &= 70
 \end{aligned}$$

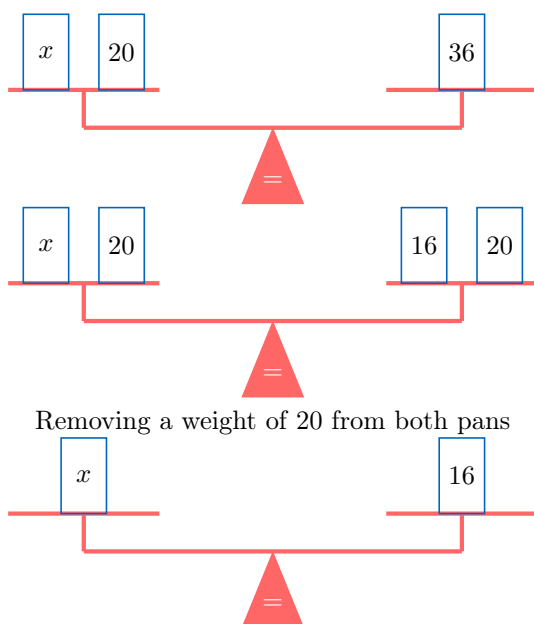
**Ex 20:** Solve for  $x$ :

$$x + 20 = 36$$

$$x = \boxed{16}$$

*Answer:*

- Balance scale:



- Equivalent equations:

$$\begin{aligned}
 x + 20 &= 36 \\
 x + 20 - 20 &= 36 - 20 & (-20) \\
 x + 0 &= 16 \\
 x &= 16
 \end{aligned}$$

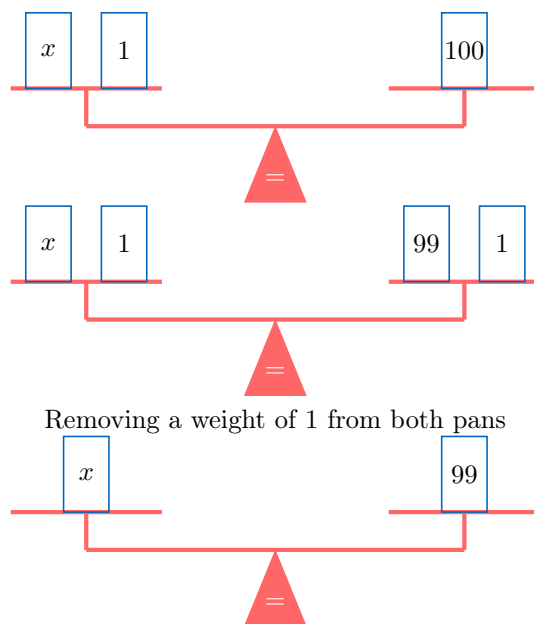
**Ex 21:** Solve for  $x$ :

$$x + 1 = 100$$

$$x = \boxed{99}$$

*Answer:*

- Balance scale:



- Equivalent equations:

$$\begin{aligned}
 x + 1 &= 100 \\
 x + 1 - 1 &= 100 - 1 & (-1) \\
 x + 0 &= 99 \\
 x &= 99
 \end{aligned}$$

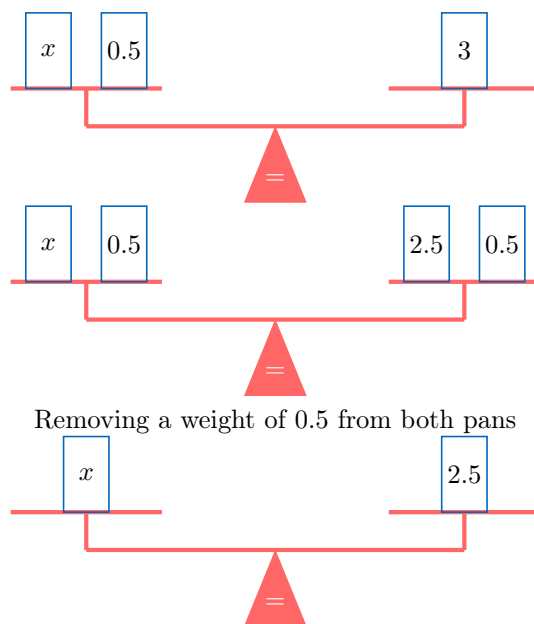
**Ex 22:** Solve for  $x$ :

$$x + 0.5 = 3$$

$$x = \boxed{2.5} \text{ (write in decimal form)}$$

*Answer:*

- Balance scale:



- Equivalent equations:

$$\begin{aligned}
 x + 0.5 &= 3 \\
 x + 0.5 - 0.5 &= 3 - 0.5 & (-0.5) \\
 x + 0 &= 2.5 \\
 x &= 2.5
 \end{aligned}$$

**Ex 23:** Solve for  $x$ :

$$x - 10 = -20$$

$$x = \boxed{-10}$$

*Answer:*

$$\begin{aligned} x - 10 &= -20 \\ x - 10 + 10 &= -20 + 10 & (+10) \\ x + 0 &= -10 \\ x &= -10 \end{aligned}$$

**Ex 24:** Solve for  $x$ :

$$x - 5 = -2$$

$$x = \boxed{3}$$

*Answer:*

$$\begin{aligned} x - 5 &= -2 \\ x - 5 + 5 &= -2 + 5 & (+5) \\ x + 0 &= 3 \\ x &= 3 \end{aligned}$$

## C.2 SOLVING EQUATIONS BY MULTIPLYING OR DIVIDING

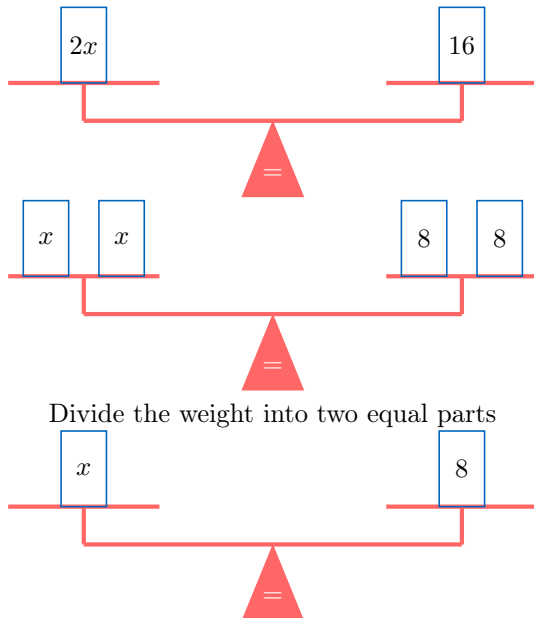
**Ex 25:** Solve for  $x$ :

$$2x = 16$$

$$x = \boxed{8}$$

*Answer:*

• Balance scale:



• Equivalent equations:

$$\begin{aligned} 2x &= 16 \\ \therefore \frac{2x}{2} &= \frac{16}{2} & (\div 2) \\ x &= 8 \end{aligned}$$

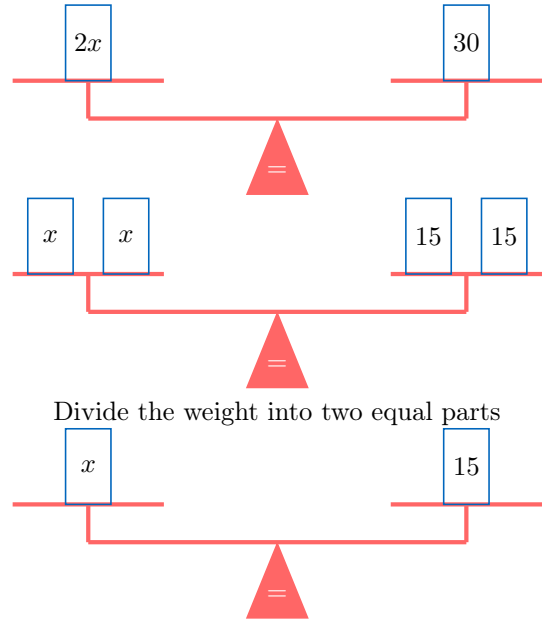
**Ex 26:** Solve for  $x$ :

$$2x = 30$$

$$x = \boxed{15}$$

*Answer:*

• Balance scale:



• Equivalent equations:

$$\begin{aligned} 2x &= 30 \\ \therefore \frac{2x}{2} &= \frac{30}{2} & (\div 2) \\ x &= 15 \end{aligned}$$

**Ex 27:** Solve for  $x$ :

$$3x = 27$$

$$x = \boxed{9}$$

*Answer:*

$$\begin{aligned} 3x &= 27 \\ \therefore \frac{3x}{3} &= \frac{27}{3} & (\div 3) \\ x &= 9 \end{aligned}$$

**Ex 28:** Solve for  $x$ :

$$\frac{x}{4} = 5$$

$$x = \boxed{20}$$

*Answer:*

$$\begin{aligned} \frac{x}{4} &= 5 \\ \therefore \frac{x}{4} \times 4 &= 5 \times 4 & (\times 4) \\ x &= 20 \end{aligned}$$

**Ex 29:** Solve for  $x$ :

$$\frac{x}{3} = \frac{1}{2}$$

$$x = \boxed{1.5} \text{ (write in decimal form)}$$

Answer:

$$\begin{aligned}\frac{x}{3} &= \frac{1}{2} \\ \therefore \frac{x}{3} \times 3 &= \frac{1}{2} \times 3 \quad (\times 3) \\ x &= \frac{3}{2} \\ x &= 1.5\end{aligned}$$

## D DOING AND UNDOING EXPRESSIONS

### D.1 DOING EXPRESSIONS

**Ex 30:** Do the expression  $3 + 5x$

$$\boxed{x} \xrightarrow{\times 5} \boxed{5x} \xrightarrow{+3} \boxed{3 + 5x}$$

Answer: To do the expression  $3 + 5x$ , follow the steps:

$$\boxed{x} \xrightarrow{\times 5} \boxed{5x} \xrightarrow{+3} \boxed{3 + 5x}$$

**Ex 31:** Do the expression  $2x + 1$

$$\boxed{x} \xrightarrow{\times 2} \boxed{2x} \xrightarrow{+1} \boxed{2x + 1}$$

Answer: To do the expression  $2x + 1$ , follow the steps:

$$\boxed{x} \xrightarrow{\times 2} \boxed{2x} \xrightarrow{+1} \boxed{2x + 1}$$

**Ex 32:** Do the expression  $5x - 1$

$$\boxed{x} \xrightarrow{\times 5} \boxed{5x} \xrightarrow{-1} \boxed{5x - 1}$$

Answer: To do the expression  $5x - 1$ , follow the steps:

$$\boxed{x} \xrightarrow{\times 5} \boxed{5x} \xrightarrow{-1} \boxed{5x - 1}$$

**Ex 33:** Do the expression  $\frac{x}{2} + 3$

$$\boxed{x} \xrightarrow{\div 2} \boxed{x/2} \xrightarrow{+3} \boxed{x/2 + 3}$$

Answer: To do the expression  $\frac{x}{2} + 3$ , follow the steps:

$$\boxed{x} \xrightarrow{\div 2} \boxed{\frac{x}{2}} \xrightarrow{+3} \boxed{\frac{x}{2} + 3}$$

**Ex 34:** Do the expression  $2 - 5x$

$$\boxed{x} \xrightarrow{\times (-5)} \boxed{-5x} \xrightarrow{+2} \boxed{2 - 5x}$$

Answer: To do the expression  $2 - 5x$ , follow the steps:

$$\boxed{x} \xrightarrow{\times (-5)} \boxed{-5x} \xrightarrow{+2} \boxed{2 - 5x}$$

**Ex 35:** Do the expression  $2(x - 3)$

$$\boxed{x} \xrightarrow{-3} \boxed{x - 3} \xrightarrow{\times 2} \boxed{2(x - 3)}$$

Answer: To do the expression  $2(x - 3)$ , follow the steps:

$$\boxed{x} \xrightarrow{-3} \boxed{x - 3} \xrightarrow{\times 2} \boxed{2(x - 3)}$$

**Ex 36:** Do the expression  $\frac{x - 3}{2}$

$$\boxed{x} \xrightarrow{-3} \boxed{x - 3} \xrightarrow{\div 2} \boxed{(x - 3)/2}$$

Answer: To do the expression  $\frac{x - 3}{2}$ , follow the steps:

$$\boxed{x} \xrightarrow{-3} \boxed{x - 3} \xrightarrow{\div 2} \boxed{\frac{x - 3}{2}}$$

### D.2 UNDOING EXPRESSIONS

**Ex 37:** Undo the expression  $2x + 1$

$$\boxed{2x + 1} \xrightarrow{-1} \boxed{2x} \xrightarrow{\div 2} \boxed{x}$$

Answer:

- To do the expression  $2x + 1$ :

$$\boxed{x} \xrightarrow{\times 2} \boxed{2x} \xrightarrow{+1} \boxed{2x + 1}$$

- To undo the expression  $2x + 1$ , perform inverse operations in the reverse order:

$$\boxed{2x + 1} \xrightarrow{-1} \boxed{2x} \xrightarrow{\div 2} \boxed{x}$$

**Ex 38:** Undo the expression  $3x - 2$

$$\boxed{3x - 2} \xrightarrow{+2} \boxed{3x} \xrightarrow{\div 3} \boxed{x}$$

Answer:

- To do the expression  $3x - 2$ :

$$\boxed{x} \xrightarrow{\times 3} \boxed{3x} \xrightarrow{-2} \boxed{3x - 2}$$

- To undo the expression  $3x - 2$ , perform inverse operations in the reverse order:

$$\boxed{3x - 2} \xrightarrow{+2} \boxed{3x} \xrightarrow{\div 3} \boxed{x}$$

**Ex 39:** Undo the expression  $\frac{x}{3} + 2$

$$\boxed{x/3 + 2} \xrightarrow{-2} \boxed{x/3} \xrightarrow{\times 3} \boxed{x}$$

Answer:

- To do the expression  $\frac{x}{3} + 2$ :

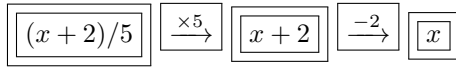
$$\boxed{x} \xrightarrow{\div 3} \boxed{\frac{x}{3}} \xrightarrow{+2} \boxed{\frac{x}{3} + 2}$$

- To undo the expression  $\frac{x}{3} + 2$ , perform inverse operations in the reverse order:

$$\boxed{\frac{x}{3} + 2} \xrightarrow{-2} \boxed{\frac{x}{3}} \xrightarrow{\times 3} \boxed{x}$$

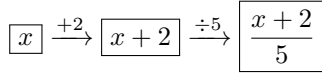


**Ex 40:** Undo the expression  $\frac{x+2}{5}$

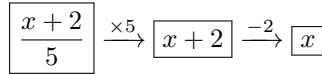


*Answer:*

- To do the expression  $\frac{x+2}{5}$ :



- To undo the expression  $\frac{x+2}{5}$ , perform inverse operations in the reverse order:



- So,

$$\begin{aligned} 2x - 4 &= 5 \\ 2x - 4 + 4 &= 5 + 4 \quad (+4) \\ 2x &= 9 \\ \frac{2x}{2} &= \frac{9}{2} \quad (\div 2) \\ x &= 4.5 \end{aligned}$$

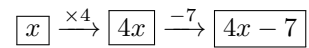
**Ex 43:** Solve for  $x$ :

$$4x - 7 = 9$$

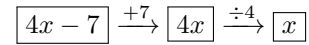
$$x = \boxed{4}$$

*Answer:*

- To **do** the expression  $4x - 7$ :



- To **undo** the expression  $4x - 7$ , do the inverse operations in reverse order:



- So,

$$\begin{aligned} 4x - 7 &= 9 \\ 4x - 7 + 7 &= 9 + 7 \quad (+7) \\ 4x &= 16 \\ \frac{4x}{4} &= \frac{16}{4} \quad (\div 4) \\ x &= 4 \end{aligned}$$

## E SOLVING LINEAR EQUATIONS

### E.1 SOLVING LINEAR EQUATIONS: LEVEL 1

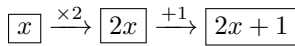
**Ex 41:** Solve for  $x$ :

$$2x + 1 = 7$$

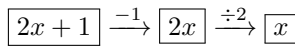
$$x = \boxed{3}$$

*Answer:*

- To **do** the expression  $2x + 1$ :



- To **undo** the expression  $2x + 1$ , do the inverse operations in reverse order:



- So,

$$\begin{aligned} 2x + 1 &= 7 \\ 2x + 1 - 1 &= 7 - 1 \quad (-1) \\ 2x &= 6 \\ \frac{2x}{2} &= \frac{6}{2} \quad (\div 2) \\ x &= 3 \end{aligned}$$

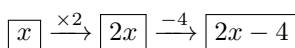
**Ex 42:** Solve for  $x$ :

$$2x - 4 = 5$$

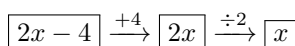
$$x = \boxed{4.5}$$

*Answer:*

- To **do** the expression  $2x - 4$ :



- To **undo** the expression  $2x - 4$ , do the inverse operations in reverse order:



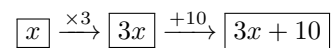
**Ex 44:** Solve for  $x$ :

$$3x + 10 = 4$$

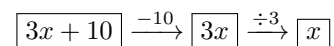
$$x = \boxed{-2}$$

*Answer:*

- To **do** the expression  $3x + 10$ :



- To **undo** the expression  $3x + 10$ , do the inverse operations in reverse order:



- So,

$$\begin{aligned} 3x + 10 &= 4 \\ 3x + 10 - 10 &= 4 - 10 \quad (-10) \\ 3x &= -6 \\ \frac{3x}{3} &= \frac{-6}{3} \quad (\div 3) \\ x &= -2 \end{aligned}$$

## E.2 SOLVING LINEAR EQUATIONS: LEVEL 2

**Ex 45:** Solve for  $x$ :

$$\frac{x-17}{3} = 10$$

$$x = \boxed{47}$$

*Answer:*

- To **do** the expression  $\frac{x-17}{3}$ :

$$\boxed{x} \xrightarrow{-17} \boxed{x-17} \xrightarrow{\div 3} \boxed{\frac{x-17}{3}}$$

- To **undo** the expression  $\frac{x-17}{3}$ , do the inverse operations in reverse order:

$$\boxed{\frac{x-17}{3}} \xrightarrow{\times 3} \boxed{x-17} \xrightarrow{+17} \boxed{x}$$

- So,

$$\begin{aligned} \frac{x-17}{3} &= 10 \\ \frac{x-17}{3} \times 3 &= 10 \times 3 \quad (\times 3) \\ x-17 &= 30 \\ x-17+17 &= 30+17 \quad (+17) \\ x &= 47 \end{aligned}$$

**Ex 46:** Solve for  $x$ :

$$\frac{x-2}{6} = \frac{2}{3}$$

$$x = \boxed{6}$$

*Answer:*

- To **do** the expression  $\frac{x-2}{6}$ :

$$\boxed{x} \xrightarrow{-2} \boxed{x-2} \xrightarrow{\div 6} \boxed{\frac{x-2}{6}}$$

- To **undo** the expression  $\frac{x-2}{6}$ , do the inverse operations in reverse order:

$$\boxed{\frac{x-2}{6}} \xrightarrow{\times 6} \boxed{x-2} \xrightarrow{+2} \boxed{x}$$

- So,

$$\begin{aligned} \frac{x-2}{6} &= \frac{2}{3} \\ \frac{x-2}{6} \times 6 &= \frac{2}{3} \times 6 \quad (\times 6) \\ x-2 &= 4 \\ x-2+2 &= 4+2 \quad (+2) \\ x &= 6 \end{aligned}$$

**Ex 47:** Solve for  $x$ :

$$4(x+2) = 40$$

$$x = \boxed{8}$$

*Answer:*

- To **do** the expression  $4(x+2)$ :

$$\boxed{x} \xrightarrow{+2} \boxed{x+2} \xrightarrow{\times 4} \boxed{4(x+2)}$$

- To **undo** the expression  $4(x+2)$ , do the inverse operations in reverse order:

$$\boxed{4(x+2)} \xrightarrow{\div 4} \boxed{x+2} \xrightarrow{-2} \boxed{x}$$

- So,

$$\begin{aligned} 4(x+2) &= 40 \\ 4(x+2) \div 4 &= 40 \div 4 \quad (\div 4) \\ x+2 &= 10 \\ x+2-2 &= 10-2 \quad (-2) \\ x &= 8 \end{aligned}$$

**Ex 48:** Solve for  $x$ :

$$\frac{2x+5}{4} = 3$$

$$x = \boxed{3.5}$$

*Answer:*

- To **do** the expression  $\frac{2x+5}{4}$ :

$$\boxed{x} \xrightarrow{\times 2} \boxed{2x} \xrightarrow{+5} \boxed{2x+5} \xrightarrow{\div 4} \boxed{\frac{2x+5}{4}}$$

- To **undo** the expression  $\frac{2x+5}{4}$ , do the inverse operations in reverse order:

$$\boxed{\frac{2x+5}{4}} \xrightarrow{\times 4} \boxed{2x+5} \xrightarrow{-5} \boxed{2x} \xrightarrow{\div 2} \boxed{x}$$

- So,

$$\begin{aligned} \frac{2x+5}{4} &= 3 \\ \frac{2x+5}{4} \times 4 &= 3 \times 4 \quad (\times 4) \\ 2x+5 &= 12 \\ 2x+5-5 &= 12-5 \quad (-5) \\ 2x &= 7 \\ \frac{2x}{2} &= \frac{7}{2} \quad (\div 2) \\ x &= 3.5 \end{aligned}$$

## F SOLVING PRODUCT OF LINEAR EQUATIONS

### F.1 SOLVING EQUATIONS USING THE NULL FACTOR LAW: LEVEL 1

**Ex 49:** Solve for  $x$ :

$$x(x+1) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{-1, 0\}$ .

Answer:

$$\begin{aligned} x(x+1) &= 0 \\ x &= 0 \text{ or } (x+1) = 0 \text{ (null factor law)} \\ x &= 0 \text{ or } x = -1 \end{aligned}$$

The set of solutions is  $\{-1, 0\}$ .

**Verification:**

- for  $x = 0$ ,  $0(0+1) = 0$
- for  $x = -1$ ,  $(-1)((-1)+1) = (-1) \times 0 = 0$

**Ex 50:** Solve for  $x$ :

$$(x+2)(x-1) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{-2, 1\}$ .

Answer:

$$\begin{aligned} (x+2)(x-1) &= 0 \\ x+2 &= 0 \text{ or } x-1 = 0 \text{ (null factor law)} \\ x &= -2 \text{ or } x = 1 \end{aligned}$$

The set of solutions is  $\{-2, 1\}$ .

**Verification:**

- For  $x = -2$ :  $(-2+2) \times (-2-1) = 0 \times (-3) = 0$
- For  $x = 1$ :  $(1+2) \times (1-1) = 3 \times 0 = 0$

**Ex 51:** Solve for  $x$ :

$$(x+6)(x-3) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{-6, 3\}$ .

Answer:

$$\begin{aligned} (x+6)(x-3) &= 0 \\ x+6 &= 0 \text{ or } x-3 = 0 \text{ (null factor law)} \\ x &= -6 \text{ or } x = 3 \end{aligned}$$

The set of solutions is  $\{-6, 3\}$ .

**Verification:**

- For  $x = -6$ :  $(-6+6) \times (-6-3) = 0 \times (-9) = 0$
- For  $x = 3$ :  $(3+6) \times (3-3) = 9 \times 0 = 0$

**Ex 52:** Solve for  $x$ :

$$(x-1)(x-2) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{1, 2\}$ .

Answer:

$$\begin{aligned} (x-1)(x-2) &= 0 \\ x-1 &= 0 \text{ or } x-2 = 0 \text{ (null factor law)} \\ x &= 1 \text{ or } x = 2 \end{aligned}$$

The set of solutions is  $\{1, 2\}$ .

**Verification:**

- For  $x = 1$ :  $(1-1) \times (1-2) = 0 \times (-1) = 0$
- For  $x = 2$ :  $(2-1) \times (2-2) = 1 \times 0 = 0$

## F.2 SOLVING EQUATIONS USING THE NULL FACTOR LAW: LEVEL 2

**Ex 53:** Solve for  $x$ :

$$(2x+6)(x+2) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{-3, -2\}$ .

Answer:

$$\begin{aligned} (2x+6)(x+2) &= 0 \\ 2x+6 &= 0 \text{ or } x+2 = 0 \text{ (null factor law)} \\ 2x &= -6 \text{ or } x = -2 \\ x &= -3 \text{ or } x = -2 \end{aligned}$$

The set of solutions is  $\{-3, -2\}$ .

**Verification:**

- For  $x = -3$ :  $(2 \times (-3) + 6)((-3) + 2) = 0 \times (-1) = 0$
- For  $x = -2$ :  $(2 \times (-2) + 6)((-2) + 2) = 2 \times 0 = 0$

**Ex 54:** Solve for  $x$ :

$$(x+2)(2x-1) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{-2, \frac{1}{2}\}$ .

Answer:

$$\begin{aligned} (x+2)(2x-1) &= 0 \\ x+2 &= 0 \text{ or } 2x-1 = 0 \text{ (null factor law)} \\ x &= -2 \text{ or } 2x = 1 \\ x &= \frac{1}{2} \end{aligned}$$

The set of solutions is  $\{-2, \frac{1}{2}\}$ .

**Verification:**

- For  $x = -2$ :  $(-2+2)(2 \times (-2) - 1) = 0 \times (-5) = 0$
- For  $x = \frac{1}{2}$ :  $(\frac{1}{2}+2)(2 \times \frac{1}{2} - 1) = \frac{5}{2} \times 0 = 0$

**Ex 55:** Solve for  $x$ :

$$\left(\frac{x}{2} - 1\right)(2x+2) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{-1, 2\}$ .

Answer:

$$\begin{aligned} \left(\frac{x}{2} - 1\right)(2x+2) &= 0 \\ \frac{x}{2} - 1 &= 0 \text{ or } 2x+2 = 0 \text{ (null factor law)} \\ \frac{x}{2} &= 1 \text{ or } 2x = -2 \\ x &= 2 \text{ or } x = -1 \end{aligned}$$

The set of solutions is  $\{-1, 2\}$ .

**Verification:**

- For  $x = -1$ :  $\left(\frac{-1}{2} - 1\right)(2 \times (-1) + 2) = \left(-\frac{1}{2} - 1\right)(-2 + 2) = \left(-\frac{3}{2}\right) \times 0 = 0$
- For  $x = 2$ :  $\left(\frac{2}{2} - 1\right)(2 \times 2 + 2) = (1 - 1) \times (4 + 2) = 0 \times 6 = 0$

**Ex 56:** Solve for  $x$ :

$$x(x-1)(x-2) = 0$$

Give your answers in increasing order:

The set of solutions is  $\{\boxed{0}, \boxed{1}, \boxed{2}\}$ .

Answer:

$$\begin{aligned} x(x-1)(x-2) &= 0 \\ x = 0 \text{ or } x-1 = 0 \text{ or } x-2 = 0 &\text{ (null factor law)} \\ x = 0 \text{ or } x = 1 \text{ or } x = 2 \end{aligned}$$

The set of solutions is  $\{\boxed{0}, \boxed{1}, \boxed{2}\}$ .

**Verification:**

- For  $x = 0$ :  $0 \times (0-1) \times (0-2) = 0 \times (-1) \times (-2) = 0$
- For  $x = 1$ :  $1 \times (1-1) \times (1-2) = 1 \times 0 \times (-1) = 0$
- For  $x = 2$ :  $2 \times (2-1) \times (2-2) = 2 \times 1 \times 0 = 0$

## G SOLVING QUADRATIC EQUATIONS IN THE FORM $x^2 = k$

### G.1 SOLVING QUADRATIC EQUATIONS IN THE FORM $x^2 = k$

**Ex 57:** Solve for  $x$ :

$$x^2 = 9$$

Give your answers in increasing order:

The set of solutions is  $\{\boxed{-3}, \boxed{3}\}$ .

Answer: We are given  $x^2 = 9$ .

- **Applying the proposition :** The solutions of this equation  $x^2 = 9$  are  $\{-\sqrt{9}, \sqrt{9}\} = \{-3, 3\}$
- **Formal resolution :** To solve for  $x$ :  

$$\begin{aligned} x^2 &= 9 \\ x^2 - 9 &= 0 \\ x^2 - 3^2 &= 0 \\ (x-3)(x+3) &= 0 \quad \text{(difference of squares)} \\ x-3 = 0 \text{ or } x+3 &= 0 \\ x = 3 \text{ or } x &= -3 \end{aligned}$$

The set of solutions is  $\{\boxed{-3}, \boxed{3}\}$ .

**Verification:**

- For  $x = -3$ :  $(-3)^2 = 9$
- For  $x = 3$ :  $(3)^2 = 9$

**Ex 58:** Solve for  $x$ :

$$x^2 = 25$$

Give your answers in increasing order:

The set of solutions is  $\{\boxed{-5}, \boxed{5}\}$ .

Answer: We are given  $x^2 = 25$ .

- **Applying the proposition :** The solutions of this equation  $x^2 = 25$  are  $\{-\sqrt{25}, \sqrt{25}\} = \{-5, 5\}$
- **Formal resolution :** To solve for  $x$ :  

$$\begin{aligned} x^2 &= 25 \\ x^2 - 25 &= 0 \\ x^2 - 5^2 &= 0 \\ (x-5)(x+5) &= 0 \quad \text{(difference of squares)} \\ x-5 = 0 \text{ or } x+5 &= 0 \\ x = 5 \text{ or } x &= -5 \end{aligned}$$

The set of solutions is  $\{\boxed{-5}, \boxed{5}\}$ .

**Verification:**

- For  $x = -5$ :  $(-5)^2 = 25$
- For  $x = 5$ :  $(5)^2 = 25$

**Ex 59:** Solve for  $x$ :

$$x^2 = 10$$

Give your answers in increasing order:

The set of solutions is  $\{\boxed{-\sqrt{10}}, \boxed{\sqrt{10}}\}$ .

Answer: We are given  $x^2 = 10$ .

- **Applying the proposition :** The solutions of this equation  $x^2 = 10$  are  $\{-\sqrt{10}, \sqrt{10}\}$
- **Formal resolution :** To solve for  $x$ :  

$$\begin{aligned} x^2 &= 10 \\ x^2 - 10 &= 0 \\ x^2 - (\sqrt{10})^2 &= 0 \\ (x-\sqrt{10})(x+\sqrt{10}) &= 0 \quad \text{(difference of squares)} \\ x-\sqrt{10} = 0 \text{ or } x+\sqrt{10} &= 0 \\ x = \sqrt{10} \text{ or } x &= -\sqrt{10} \end{aligned}$$

The set of solutions is  $\{\boxed{-\sqrt{10}}, \boxed{\sqrt{10}}\}$ .

**Verification:**

- For  $x = -\sqrt{10}$ :  $(-\sqrt{10})^2 = 10$
- For  $x = \sqrt{10}$ :  $(\sqrt{10})^2 = 10$

**Ex 60:** Solve for  $x$ :

$$x^2 - 3 = 0$$

Give your answers in increasing order:

The set of solutions is  $\{\boxed{-\sqrt{3}}, \boxed{\sqrt{3}}\}$ .

*Answer:* We are given  $x^2 - 3 = 0$ .

- **Applying the proposition :** The solutions of this equation  $x^2 = 3$  are

$$\{-\sqrt{3}, \sqrt{3}\}$$

- **Formal resolution :** To solve for  $x$ :

$$x^2 - 3 = 0$$

$$x^2 - (\sqrt{3})^2 = 0$$

$$(x - \sqrt{3})(x + \sqrt{3}) = 0 \quad (\text{difference of squares})$$

$$x - \sqrt{3} = 0 \quad \text{or} \quad x + \sqrt{3} = 0$$

$$x = \sqrt{3} \quad \text{or} \quad x = -\sqrt{3}$$

The set of solutions is  $\boxed{\{-\sqrt{3}, \sqrt{3}\}}$ .

**Verification:**

- For  $x = -\sqrt{3}$ :  $(-\sqrt{3})^2 - 3 = 3 - 3 = 0$
- For  $x = \sqrt{3}$ :  $(\sqrt{3})^2 - 3 = 3 - 3 = 0$