

TRANSFORMATIONS

A TYPES OF TRANSFORMATIONS

Transformations are ways to move, flip, or turn a shape.

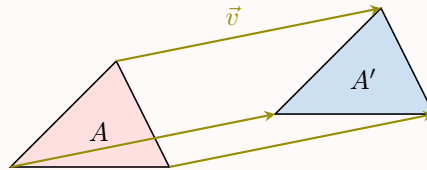
Definition Object and Image

When a transformation is applied to a shape, the input shape is called the **object**. The output shape after the transformation is called the **image**.

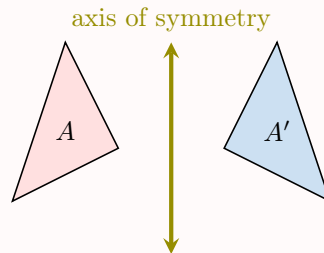
Definition Types of Transformations

There are several types of transformations, including:

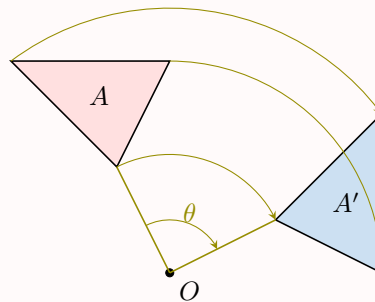
- **Translation:** Slides the shape to a new position without changing its shape, size, or the direction it faces.



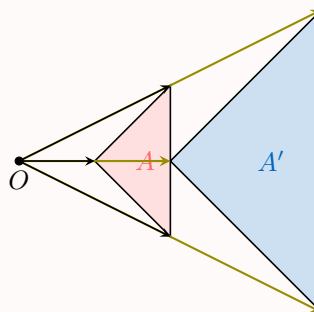
- **Reflection:** Flips the shape over a line (like a mirror), creating a mirror image.



- **Rotation:** Turns the shape around a point by a certain angle.



- **Homothety:** Enlarges or reduces the shape by a scale factor from a center point, keeping the shape similar.

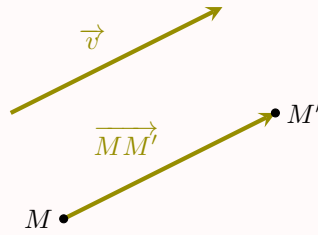


B TRANSLATION

A **translation** moves a figure from one place to another. Every point on the figure moves the same distance in the same direction.

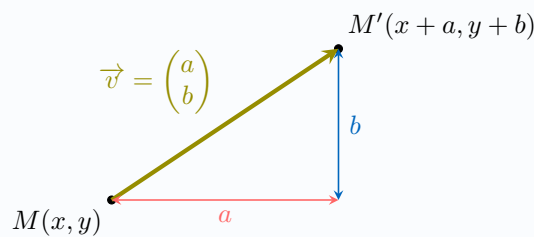
Definition Translation

A translation by the vector \vec{v} maps a point M to its image M' such that $\overrightarrow{MM'} = \vec{v}$.



Proposition Coordinates of the Image Point

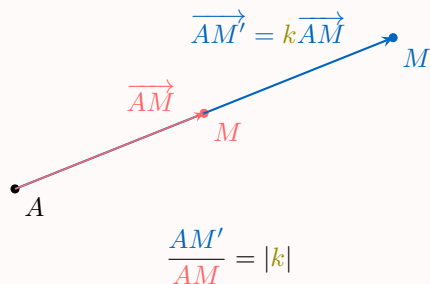
In a coordinate system, if the point M has coordinates (x, y) and the translation vector is $\vec{v} = \begin{pmatrix} a \\ b \end{pmatrix}$, then the image point M' has coordinates $(x + a, y + b)$.



C HOMOTHETY

Definition Homothety

A **homothety** with center A and scale factor k maps a point M to the point M' such that M' is obtained by translating the point A by the vector $k\overrightarrow{AM}$.



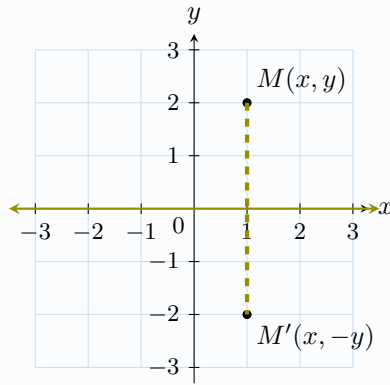
Proposition Coordinates of the Image Point

In a coordinate system, if the center A has coordinates (a, b) , the point M has coordinates (x, y) , and the scale factor is k , then the image point M' has coordinates $(a + k(x - a), b + k(y - b))$.

D SPECIFIC REFLECTIONS

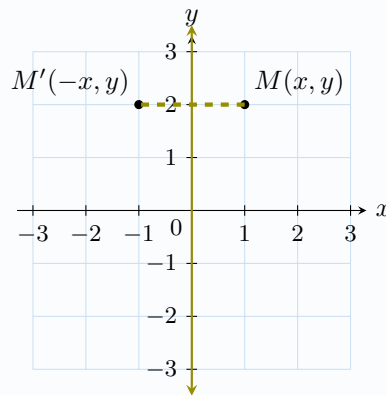
Proposition Reflection over the x -axis

The image of the point $M(x, y)$ under the reflection over the x -axis is $M'(x, -y)$.



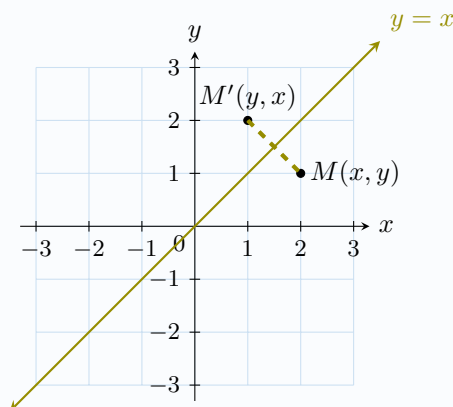
Proposition Reflection over the y -axis

The image of the point $M(x, y)$ under the reflection over the y -axis is $M'(-x, y)$.



Proposition Reflection over the line $y = x$

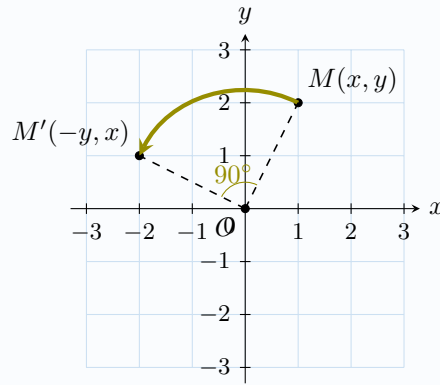
The image of the point $M(x, y)$ under the reflection $M_{y=x}$ over the line $y = x$ is $M'(y, x)$.



E SPECIFIC ROTATIONS

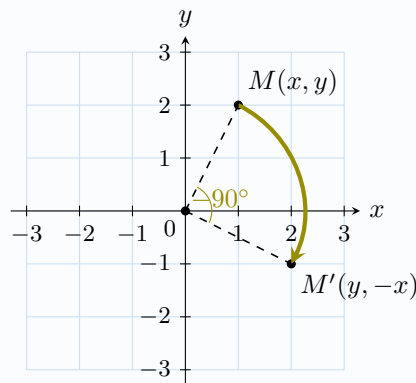
Proposition Rotation of 90°

The image of the point $M(x, y)$ under the rotation of 90° (counterclockwise) around the origin is $M'(-y, x)$.



Proposition Rotation of -90°

The image of the point $M(x, y)$ under the rotation of -90° (clockwise) around the origin is $M'(y, -x)$.



Proposition Rotation of 180°

The image of the point $M(x, y)$ under the rotation of 180° around the origin is $M'(-x, -y)$.

